

Growing an ω-Automaton Library

Alexandre Duret-Lutz (EPITA, France)

A platform for manipulation of LTL formulas and ω -automata. With three interfaces.

C++17 library

Command-line tools



A platform for manipulation of LTL formulas and ω -automata. With three interfaces. E.g. convert an LTL formula into a neverclaim for Spin:



2/23

A platform for manipulation of LTL formulas and ω -automata. With three interfaces. E.g. convert an LTL formula into a neverclaim for Spin:



C++17 library

Command-line tools

Python bindings

A platform for manipulation of LTL formulas and ω -automata. With three interfaces. E.g. convert an LTL formula into a neverclaim for Spin:



C++17 library

- Command-line tools
- % ltl2tgba --spin GFa

Python bindings

A platform for manipulation of LTL formulas and ω -automata. With three interfaces. E.g. convert an LTL formula into a neverclaim for Spin:



C++17 library

Command-line tools

```
% ltl2tgba --spin GFa
```

Python bindings

import **spot**

a = spot.translate('GFa', 'buchi', 'sbacc')
print(a.to_str('spin'))

 With graphical representations in Jupyter



🔋 Lind-Nielsen. BuDDy: A binary decision diagram package, 1999. 👓 👐









🔋 Kant et al. LTSmin: High-performance language-independent model checking. TACAS'15. 💶 3/23



1 Model checking library (2003–2012)

- using TGBA for model checking
- pure C++ library
- no tools (except for the test suite)



Duret-Lutz and Poitrenaud. Spot: an extensible model checking library using transition-based generalized Büchi automata. MASCOTS'04. • doi

1 Model checking library (2003–2012)

- using TGBA for model checking
- pure C++ \ibrary
- no tools (except for the test suite)



Duret-Lutz and Poitrenaud. Spot: an extensible model checking library using transition-based generalized Büchi automata. MASCOTS'04. • doi

1 Model checking library (2003–2012)

- using TGBA for model checking
- pure C++ \ibrary
- no tools (except for the test suite)



Fig. 7 illustrates how we have connected Spot to GreatSPN³. GreatSPN can produce a symbolic reachability graph (SRG) for a Colored Petri net by exploiting its symmetries [19]. We have implemented this interface as a tgba subclass whose methods simply delegate their work to the corresponding procedures of GreatSPN. From the point of view of Spot, an SRG appears as any other TGBA.



Duret-Lutz and Poitrenaud. Spot: an extensible model checking library using transition-based generalized Büchi automata. MASCOTS'04. • doi

1 Model checking library (2003–2012)

- using TGBA for model checking
- pure C++ library
- no tools (except for the test suite)

2 Platform for LTL manip. and model checking (2012–2015)

- tools with LTL/PSL input
- no tool reading TGBA by lack of exchange format

1 Model checking library (2003 - 2012)

- using TGBA for model checking
- pure C++ library
- no tools (except for the test suite)

Platform for LTL manip. and model checking (2012-2015)

- tools with LTL/PSL input
- no tool reading TGBA by lack of exchange format

3 Platform for LTL and ω -automata (2016–)

- major rewrite HOA format
- more tools

- Jupyter support



- Duret-Lutz et al. Spot 2.0 a framework for LTL and ω -automata manipulation. ATVA'16.
- Babiak et al. The Hanoi Omega-Automata format. CAV'15.

1 Model checking library (2003–2012)

- using TGBA for model checking
- pure C++ library
- no tools (except for the test suite)

2 Platform for LTL manip. and model checking (2012–2015)

- tools with LTL/PSL input
- no tool reading TGBA by lack of exchange format

3 Platform for LTL and ω -automata (2016–)

- HOA format
- more tools

- major rewrite
- Jupyter support

4 New application: Synthesis

- build on existing features
- improves existing features
- adds games, mealy machines

What I will present

1 Model checking library (2003–2012)

A bug!

2 Platform for LTL manip. and model checking (2012–2015)

- command-line tools
- SAT-based minimization

3 Platform for LTL and ω -automata (2016–)

- Jupyter visualizations
- Emerson-Lei acceptance conditions

4 New application: Synthesis
 > ltlsynt, ACD
 > ltlfsynt, MTDFA

A memorable bug

(Reported in 2007; fixed in 2009.)

Kristin Rozier's paper

[Spin'07] LTL Satisfiability Checking Kristin Y. Rozier¹ * and Moshe Y. Vardi² NASA Langley Research Center, Hampton, Virginia 23681. Kristin.Y.Rozier@nasa.gov ² Rice University, Houston, Texas 77005, vardi@cs.rice.edu

Abstract. We report here on an experimental investigation of LTL satisfiability checking via a reduction to model checking. By using large LTL formulas, we offer challenging model-checking benchmarks to both explicit and symbolic model checkers. For symbolic model checking, we use both CadenceSMV and NuSMV. For explicit model checking, we use SPIN as the search engine, and we test essentially all publicly available LTL translation tools. Our experiments result in two major findings. First, most LTL translation tools are research prototypes and cannot be considered industrial quality tools. Second, when it comes to LTL satisfiability checking, the symbolic approach is clearly superior to the explicit approach.

Kristin Rozier's paper



▶ do

Kristin Rozier's paper

[Spin'07]	
LTL Sat	isfiability Checking
Kristin Y. F ¹ NASA Langley Research Center, I ² Rice University, He	From: Kristin Yvonne Rozier Subject: experiments with Spot Date: 16 Aug 2007 []
Abstract. We report here of ity checking via a reduction we offer challenging model- model checkers. For symbol NuSMV. For explicit model test essentially all publicly a in two major findings. Firs and cannot be considered in satisfiability checking, the approach.	At SPIN/CAV this year, it was suggested that you might be interested in seeing the few LTL formulas I found which trigger unexpected behavior from Spot. Here is a summary of those formulas. []

 C_n is a 2-variable LTL formula describing a loop over all values of an *n*-bit counter.

 C_n is a 2-variable LTL formula describing a loop over all values of an *n*-bit counter.

 $\mathsf{XXX}\neg b)\,\mathsf{U}\,(m\lor(\neg b\land\neg m\land\mathsf{X}(\mathsf{XX}b\land((\neg m\land(b\leftrightarrow\mathsf{XXX}b))\,\mathsf{U}\,m)))))))$

 C_n is a 2-variable LTL formula describing a loop over all values of an *n*-bit counter.

 $C_3 = \neg b \land m \land \mathsf{G}(m \to \mathsf{X}(\neg m \land \mathsf{X}(\neg m \land \mathsf{X}m))) \land \mathsf{X}(\neg b \land \mathsf{X} \neg b) \land \mathsf{G}((\neg b \land m) \to \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}(\neg m \land \mathsf{X}m))) \land \mathsf{X}(\neg b \land \mathsf{X} \neg b) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}(\neg m \land \mathsf{X}))) \land \mathsf{X}(\neg b \land \mathsf{X} \neg b) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{G}(m \land \mathsf{X}))$

 $\mathsf{XXX}\neg b)\,\mathsf{U}\,(m\lor(\neg b\land\neg m\land\mathsf{X}(\mathsf{XX}b\land((\neg m\land(b\leftrightarrow\mathsf{XXX}b))\,\mathsf{U}\,m)))))))$



The mininal automaton for C_n has $n2^n$ states.

 C_n is a 2-variable LTL formula describing a loop over all values of an *n*-bit counter.

 $C_3 = \neg b \land m \land \mathsf{G}(m \to \mathsf{X}(\neg m \land \mathsf{X}(\neg m \land \mathsf{X}m))) \land \mathsf{X}(\neg b \land \mathsf{X} \neg b) \land \mathsf{G}((\neg b \land m) \to \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}(\neg m \land \mathsf{X}m))) \land \mathsf{X}(\neg b \land \mathsf{X} \neg b) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}(\neg m \land \mathsf{X}))) \land \mathsf{X}(\neg b \land \mathsf{X} \neg b) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{X}) \land \mathsf{G}(m \land \mathsf{X})) \land \mathsf{G}(m \land \mathsf{G}(m \land \mathsf{X}))$

 $\mathsf{XXX}\neg b)\,\mathsf{U}\,(m\lor(\neg b\land\neg m\land\mathsf{X}(\mathsf{XX}b\land((\neg m\land(b\leftrightarrow\mathsf{XXX}b))\,\mathsf{U}\,m)))))))$



The mininal automaton for C_n has $n2^n$ states.

110

 C_n is a 2-variable LTL formula describing a loop over all values of an *n*-bit counter.

001

Kristin's issue with Spot 0.3:

100

000





 C_{10} needs at least 10240 states and (back then) Spot already needs a couple of minutes to build the erroneous automaton. $b\bar{m}$ $b\bar{m}$ $b\bar{m}$ $b\bar{m}$ $b\bar{m}$

The mininal automaton for C_n has $n2^n$ states.

010

 C_n is a 2-variable LTL formula describing a loop over all values of an *n*-bit counter.

{

bm

110

3

Kristin's issue with Spot 0.3:

 C_1 SAT C_5 SAT C_9 SAT C_2 SAT C_6 SAT C_{10} UNSAT C_3 SAT C_7 SAT C_{11} SAT C_4 SAT C_8 SAT C_{12} SAT

 C_{10} needs at least 10240 states and then) Spot already needs a couple o utes to build the erroneous automate

bm

100

bm

000

The one-character fix!

```
bool operator<(const formula* left,</pre>
```

```
const formula* right)
```

```
size_t l = left->hash();
size_t r = right->hash();
if (1 != r)
```

```
+ if (l != r)
```

```
return l < r;
```

```
return left->dump() < right->dump();
```

The mininal automaton for C_n has $n2^n$ states.

010

bm

- I'm now very picky about the font I use in my terminal and editor. (losevka is great! ••••••)
- Realized that the representation of LTL formulas in Spot 0.4 was really inefficient.
- ► Divided translation time by ≈ 3 after fixing the bug, by improving formula representations.
- Today C_n can be generated by Spot's genltl tool.



Command-line Tools

Objectives:

- Easy access to Spot's algorithms
- Providing convenient tools for day-to-day experiments
- Support streaming (a.k.a., pipelining) and scripting (i.e., useful exit codes)
- Have coherent options among tools
- Have good defaults
- Have good error reporting

SAT-based minimization of deterministic TGBA

From LTL to Minimal D[T][G]BA

Output: DBA. (Ehlers' setup.)





Ehlers. Minimising deterministic Büchi automata precisely using SAT solving. SAT'10. 🚥



From LTL to Minimal D[T][G]BA

Output: DBA. (Ehlers' setup.)



Klein and Baier. On-the-fly stuttering in the construction of determ. ω-automata. CIAA'07.
 Krishnan, Puri, and Brayton. Determ. ω-automata vis-a-vis determ. Büchi automata. ISAAC'94.

From LTL to Minimal D[T][G]BA

Output: DBA.



Dax, Eisinger, and Klaedtke. Mechanizing the powerset construction for restricted classes of ω-automata. ATVA'07. • doi: de

12/23
Output: DTBA.



Output: DTBA.



Output: DTBA.



Dax, Eisinger, and Klaedtke. Mechanizing the powerset construction for restricted classes of ω-automata. ATVA'07. • doi: de

12/23

Output: DTBA.



Dax, Eisinger, and Klaedtke. Mechanizing the powerset construction for restricted classes of ω -automata. ATVA'07.

12/23

Output: DTGBA (m > 1) or DTBA (m = 1).



Output: DTGBA (m > 1) or DTBA (m = 1). Our setup.



Baarir and Duret-Lutz. Mechanizing the minimization of deterministic generalized Büchi automata. FORTE'14. • ••••

Spot 2 HOA + Jupyter \implies major rewrite

Babiak et al. The Hanoi Omega-Automata format. CAV'15. 🚥



<u>e</u> lin	nort at	nin	lloation
500			

ltl2dstar 0.5.3	PRISM 4.3	iboafnargor	
ltl3ba 1.1.2	Rabinizer 3.1	Suppostance	
lt13dra 0.2.2	Spot 1.99.2	cppiloai pai sei	





Original motivations

Unify output formats for different tools/acceptance conditions





Original motivations

Unify output formats for different tools/acceptance conditions



Resulting challenge

Can we build tools that process automata with arbitrary acceptance conditions?





















automata simplifications

Most of Spot's simplifications have been generalized already.

automata simplifications

Most of Spot's simplifications have been generalized already.

complementation

Trivial on any deterministic ω -automata. What about non-deterministic ω -automata?



automata simplifications

Most of Spot's simplifications have been generalized already.

complementation

Trivial on any deterministic ω -automata. What about non-deterministic ω -automata?

emptiness check

Easy for "Fin-less acceptance".

Generic Emptiness Check implemented since Spot 2.7.



automata simplifications

Most of Spot's simplifications have been generalized already.

complementation

Trivial on any deterministic ω -automata. What about non-deterministic ω -automata?

emptiness check

Easy for "Fin-less acceptance".

Generic Emptiness Check implemented since Spot 2.7.

acceptance conversions

Many are implemented.

(Jupyter demo)



Reactive Synthesis

Reactive Synthesis in a Nutshell

A reactive controller produces output as a reaction to its input

input signals
$$\left\{ \begin{array}{ccc} \underline{\bar{a}} & a & \underline{\bar{a}} & \dots \\ \underline{\bar{b}} & \underline{\bar{b}} & b & b & \dots \end{array} \xrightarrow{\overline{x}} \overline{x} & x & x & \dots \\ \overline{y} & \overline{y} & \overline{y} & \overline{y} & \dots \end{array} \right\}$$
 output signals



Reactive Synthesis in a Nutshell

A reactive controller produces output as a reaction to its input

put signals
$$\left\{ \begin{array}{ccc} \bar{a} & a & \bar{a} & \dots \\ \hline \bar{b} & \bar{b} & b & \dots \end{array} \xrightarrow{\bar{x}} \bar{x} & x & x & \dots \\ \hline \bar{y} & y & \bar{y} & \bar{y} & \dots \end{array} \right\}$$
 output signals

The reactive synthesis problems

Given a specification relating input signals and output signals over time: **Realizability:** decide if a controller exist; **Synthesis:** construct it.



Reactive Synthesis in a Nutshell

A reactive controller produces output as a reaction to its input

put signals
$$\left\{ \begin{array}{c} \bar{a} & a & \bar{a} \\ \bar{b} & \bar{b} & b \\ \hline \bar{b} & \bar{b} & b \\ \hline \end{array} \right\} \xrightarrow{\bar{x}} x x x x \dots \\ \xrightarrow{\bar{y}} \overline{y} \overline{y} \overline{y} \dots \end{array}$$
 output signals

The reactive synthesis problems

in

Given a specification relating input signals and output signals over time: **Realizability:** decide if a controller exist; **Synthesis:** construct it.

LTL Synthesis Competition

the specification is an LTL formula, over ω-words such as "ābxy; abxy; abxy;..."

the controller should be an And-Inverter Graph











Renkin et al. Effective reductions of Mealy machines. FORTE'22.









Křetínský et al. Index appearance record with preorders. Acta Informatica, 2021. 🗖








Procedures implemented in Spot.

Komárková and Křetínský. Rabinizer 3: Safraless translation of LTL to small deterministic automata. ATVA'14.



Esparza et al. From LTL and limit-deterministic Büchi automata to deterministic parity automata. TACAS'17. • doi



 Müller and Sickert. LTL to deterministic Emerson-Lei automata. GandALF'17. Colo
 Major et al. Itl3tela: LTL to small deterministic or nondeterministic Emerson-Lei automata. ATVA'19. Colo



Renkin, Duret-Lutz, and Pommellet. Practical "paritizing" of Emerson-Lei automata. ATVA'20.
 Δioding. Optimal bounds for transformations of ω-automata. FSTTCS'99.
 Δioding. Optimal bounds for transformations of ω-automata.
 Δioding. Optimal bounds for transformations of ω-automata.
 Δioding. Optimal bounds for transformations of ω-automata.
 Δioding. Optimal bounds for transformations of ω-automata.



Casares, Colcombet, and Fijalkow. Optimal transformations of games and automata using Muller conditions. ICALP'21. • • • •

Casares et al. Practical applications of the Alternating Cycle Decomposition. TACAS'22. 1/23

(Jupyter demo)



What I did present

1 Model checking library (2003–2012)

A bug!

2 Platform for LTL manip. and model checking (2012–2015)

- command-line tools
- SAT-based minimization

3 Platform for LTL and ω -automata (2016–)

- Jupyter visualizations
- Emerson-Lei acceptance conditions

