Introduction to Computation and Complexity Exercise Sheet 5

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Exercise 1

Prove that $ISOMORPHISM = \{G \# H \mid G \text{ and } H \text{ are isomorphic graphs.}\} \in NP$. Note that there is no known proof of this problem being NP-complete.

Hint 1: design a binary encoding of graphs.

Hint 2: find a certificate.

Exercise 2

Prove that SUBSETSUM = $\{\{x_1, \ldots, x_n\} \ \# \ t \mid \exists i_1, \ldots, i_k \in \{1, \ldots, n\} \text{ such that } \forall j \neq j', i_j \neq i_{j'} \text{ and } x_{i_1} + \ldots + x_{i_k} = t\} \in NP.$