Introduction to Computation and Complexity Exercise Sheet 2

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December 12, 2023

Exercise 1

Design a Turing machine M recognizing the language $\{ww^R \mid w \in \Sigma^*\}$, where w^R is the reverse of the word w.

Exercise 2

Design a Turing machine M recognizing the language $\{a^n b^n c^n \mid n \ge 1\}$.

Exercise 3

Let L be a language such that \overline{L} is not RE. Prove that:

$$L' = \{0w \mid w \in L\} \cup \{1w \mid w \in \overline{L}\}$$

is not RE.

Exercise 4

Let L_1, \ldots, L_n be a collection of RE languages that is also a *partition* of Σ^* , i.e. $\forall i \neq j, L_i \cap L_j = \emptyset$ and $L_1 \cup \ldots \cup L_n = \Sigma^*$. Prove that for $i = 1, \ldots n$, the language L_i is recursive.