



History



Paradigm



Characteristics



Summary

Functional Approaches to Programming

~ Introduction ~

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Characteristics of the Functional Approach

Summary





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1930: Lambda-Calculus (Alonzo Church)

- ▶ Formel system for calculus (*Top-Down*)
- ▶ Rules
 - ▶ Variable: x
 - ▶ Abstraction: $(\lambda x.M)$
 - ▶ Application: (MN)
- ▶ Operators
 - ▶ α -conversion: $(\lambda x.M[x]) \rightarrow (\lambda y.M[y])$
 - ▶ β -reduction: $((\lambda x.M)E) \rightarrow (M[x := E])$
- ▶ 1937: Proof of Turing-completeness
 - ▶ [Turing, 1937]
- ▶ 1920 / 1930: Combinatorial Logic, equivalent theory
 - ▶ [Curry, 1958]



Princeton

1958: Lisp (John McCarthy)

- ▶ Origin (LISP) [McCarthy, 1960]
 - ▶ MIT AI Lab, IBM 700/7000
 - ▶ 2nd oldest high level language
 - ▶ 1st functional language
 - ▶ lambda-calculus + recursion
 - ▶ Multi-paradigm / Homoiconic
- ▶ Dialects / Chronology
 - ▶ 1975: Scheme / Lisp Machines
 - ▶ 1980: Common Lisp (ANSI Standard 1994)
 - ▶ 1985: Emacs Lisp
 - ▶ 2005: Clojure
 - ▶ 2010: Racket



Futura Science

Other Languages

- ▶ Historical
 - ▶ IPL (1956) *Assembly level, very imperative*
 - ▶ APL (Iverson, 1960), FP (Backus, 1977) [Backus, 1978]
 - ▶ ML (Milner, 1973), Standard ML, Caml / OCaml (Leroy, 1996)
 - ▶ Miranda (Turner, 1985), Haskell (1990)
- ▶ More recent *Object / Functional mix*
 - ▶ Scala (Odersky, 2004)
 - ▶ F# (M\$, 2005)
- ▶ In the mix
 - ▶ Python, Ruby, JavaScript, Julia, etc.
- ▶ Back to Functional
 - ▶ Lambda-expressions in C++11 / Java 8





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A Programming Paradigm

- ▶ **Reminders on the concept of paradigm**
 - ▶ Affects the *expressivity* of a language
 - ▶ Affects the *thought* process in a language
 - ▶ Porosity
- ▶ **The functional paradigm**
 - ▶ Expression (vs. Instruction)
 - ▶ Evaluation (vs. Execution)

“What to do” rather than “How to do it”



From Imperative to Functional

“The sum of the squares of the integers between 1 and N ”

C (imperative)

```
int ssq (int n)
{
    int i = 1, a = 0;
loop:
    a += i*i; i += 1;
    if (i <= n+1)
        goto loop;

    return a;
}
```

C (recursive)

```
int ssq (int n)
{
    if (n == 1)
        return 1;
    else
        return n*n + ssq (n-1);
}
```

Lisp

```
(defun ssq (n)
  (if (= n 1)
      1
      (+ (* n n) (ssq (1- n)))))
```

Haskell

```
ssq :: Int -> Int
ssq 1 = 1
ssq n = n*n + ssq (n-1)
```

- ▶ Clarity
- ▶ Concision



Imperative Upside Down

“The square root of the sum of the squares of a and b”

C (imperative)

```
float hypo (float a, float b)
{
    float a2 = a*a;
    float b2 = b*b;
    float s = a2 + b2;

    return sqrt (s);
}
```

C (less imperative)

```
float hypo (float a, float b)
{
    return sqrt (a*a + b*b);
}
```

Haskell

```
hypo :: Float -> Float -> Float
hypo a b = sqrt (a*a + b*b)
```

Lisp

```
(defun hypo (a b)
  (sqrt (+ (* a a) (* b b))))
```

Mais...

Haskell (100% prefix)

```
hypo :: Float -> Float -> Float
hypo a b = sqrt ((+) ((* a a) ((* b b)))
```





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Higher Order Functions

Aka 1st order, 1st class

▶ **Christopher Strachey** [Strachey, 72]

- ▶ naming (variables)
- ▶ aggregation (structures)
- ▶ anonymous manipulation
- ▶ function argument
- ▶ function return value
- ▶ dynamic construction
- ▶ ...

▶ **Advantage:** increased expressivity (clarity, concision, etc.)

▶ Example: “mapping”

Lisp

```
(mapcar #'sqrt '(1 2 3 4 5))
```

Haskell

```
map sqrt [1..5]
```



Evaluation Principles

▶ **Question:** when to compute the value of an expression ?

▶ **Réponses**

1. Beforehand (Lisp, *strict evaluation*)
2. On demand (Haskell, *lazy evaluation*)

▶ Example:

Lisp

```
(defun intlist (s) ;; KO
  (cons s (intlist (1+ s))))
```

Haskell

```
intlist :: Int -> [ Int ] -- OK
intlist s = s : intlist (s + 1)
```

▶ **Advantage:** increased expressivity (clarity, concision, etc.)

▶ **Constraint:** purely functional only



Pure Functional Programming

The function, in the mathematical sense

$$ssq(x) = \begin{cases} 1 & \text{si } x = 1, \\ x^2 + ssq(x - 1) & \text{sinon.} \end{cases}$$

Haskell

```
ssq :: Int -> Int
ssq 1 = 1
ssq n = n*n + ssq (n-1)
```

▶ Function

- ▶ Imperative: (procedure) sequence of computations with *side effects*, possibly with a return value
- ▶ Purely Functional: computation of a (return) value depending on input values (arguments)

▶ Variable

- ▶ Imperative: storage of values which may *vary* over time (mutation)
- ▶ Purely Functional: unknown or arbitrary (but constant) value



Advantages of Purity

Purity \implies (more) safety

- ▶ **Parallelism**
 - ▶ Cf. Erlang
- ▶ **Function-local semantics**
 - ▶ Local tests / Local bugs
- ▶ **Program proofs**



Formal Proofs

Mathematical Induction

“Proove (please) that $\forall N, \text{ssq}(N) > 0$ ”

Purely functional

Haskell

```
ssq :: Int -> Int
ssq 1 = 1
ssq n = n*n + ssq (n-1)
```

- ▶ It's true at rank 1
- ▶ Suppose it's true at rank $N - 1$...

Imperative

C

```
int ssq (int n)
{
    int i = 1, a = 0;
loop:
    a += i*i; i += 1;
    if (i <= n+1)
        goto loop;

    return a;
}
```

- ▶ Ugh...

Limitations of the Mathematical Formalism

How to express the concept of “square root” ?

$$\text{sqrt}(x) = y \mid \begin{cases} y > 0 \\ y^2 = x \end{cases}$$

Lisp

```
(defun sqrt (x) ???)
```

Haskell

```
sqrt :: Float -> Float
sqrt x = ???
```

Lisp

```
(defun sqrtp (s x)
  (and (> s 0)
       (= (* s s) x)))
```

Haskell

```
sqrtp :: Float -> Float -> Bool
sqrtp s x = s > 0 && s*s == x
```

- ▶ By the end of the day, you still need to explain *how to do it*...
- ▶ But you just postpone the question: declarative or imperative ?





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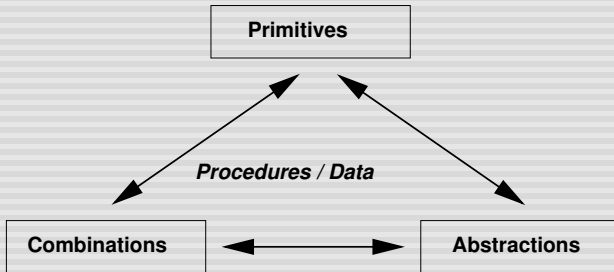
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Benefits of the Functional Approach

The 3 characteristics of (good) languages



- ▶ Less distinction between procedures and data
- ▶ More power in combination
- ▶ More power in abstraction





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Bibliography





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