

# MLRF Lecture 03

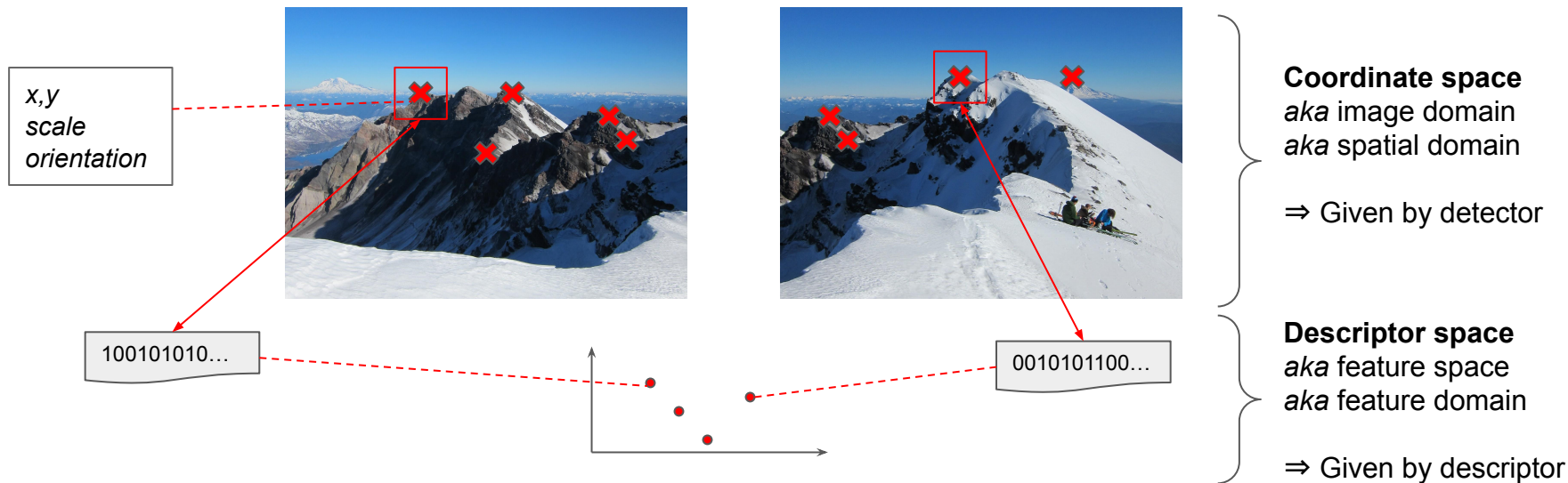
J. Chazalon, LRDE/EPITA, 2021

# Descriptors matching and indexing

Lecture 03 part 03

# Introduction

*Given some keypoints in image 1, what are the more similar ones in image 2?*



This is a **nearest neighbor problem in descriptor space** (this lecture part).

This is also a **geometrical problem in coordinate space** (next lecture parts).

# Matching

# Matching problem

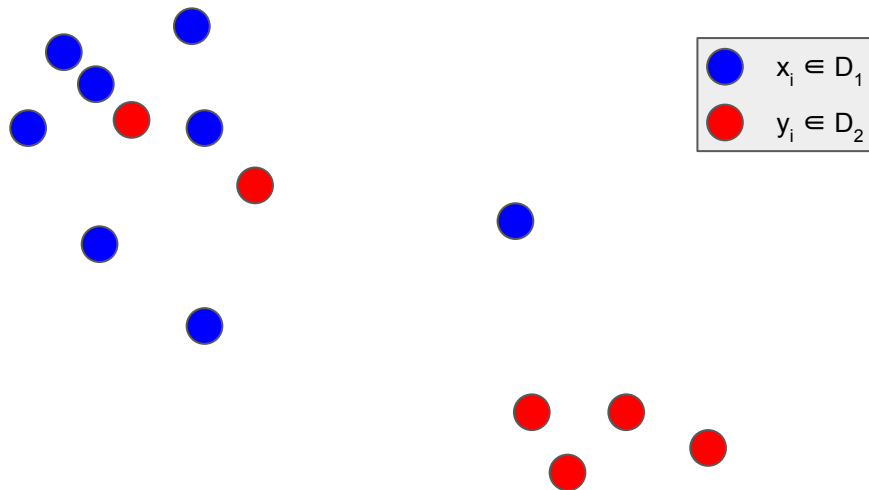
Goal: given two sets of descriptors, find the best matching pairs.

Need a **distance/norm**: depends on the descriptor

- Distribution (histogram)? Statistics?
- Data type?
  - Float, integers: Euclidean, cosine...
  - Binary: Hamming...

# 1-way matching

For each  $x_i$  in the set of descriptors  $D_1$ , find the closest element  $y_i$  in  $D_2$ .

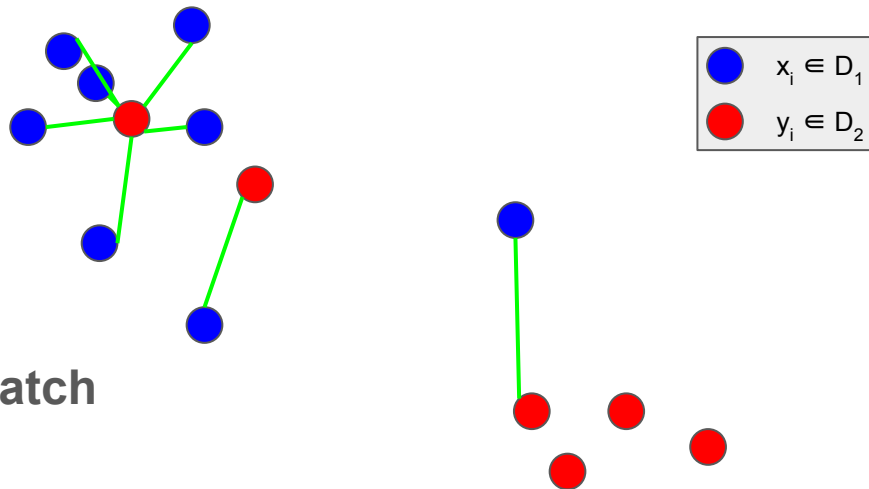


# 1-way matching

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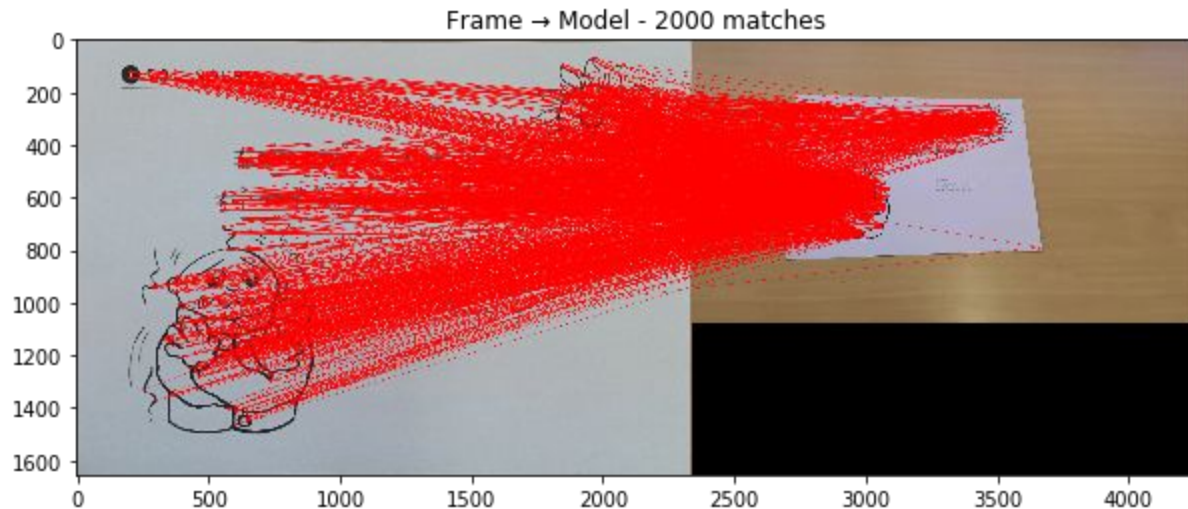
We have a match  $m(x_i, y_i)$  for each  $x_i$

Many  $y_i$  in  $D_2$  may **not belong to any match**



# 1-way matching

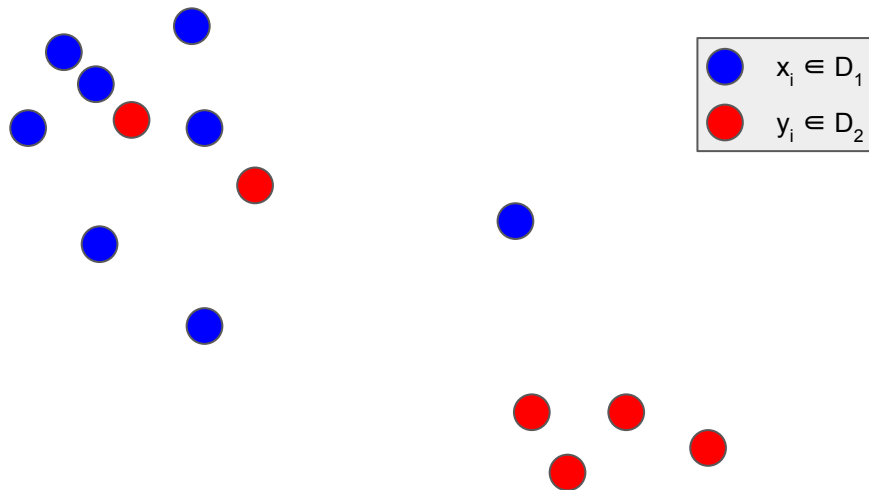
Example from next practice session





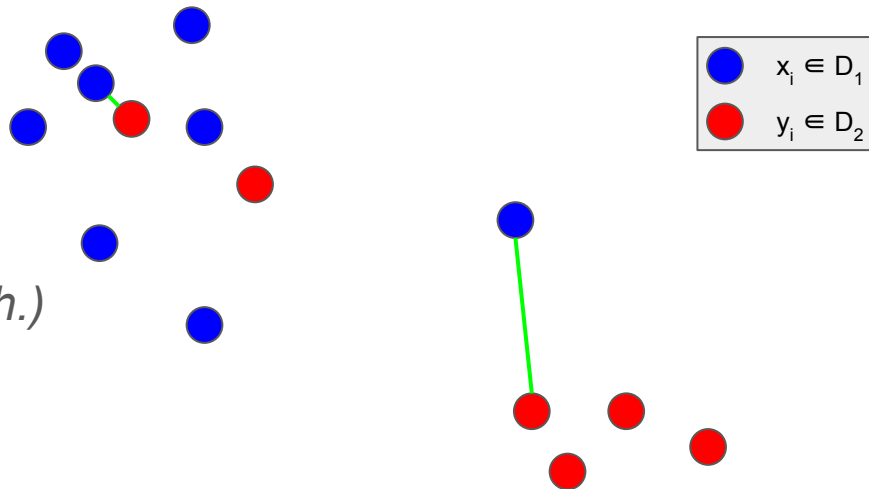
# Symmetry test *aka* cross check *aka* 2-way matching

For each  $x_i$  in the set of descriptors  $D_1$ , find the closest element  $y_i$  in  $D_2$  such as  $x_i$  is **also the closest** element to  $y_i$ .



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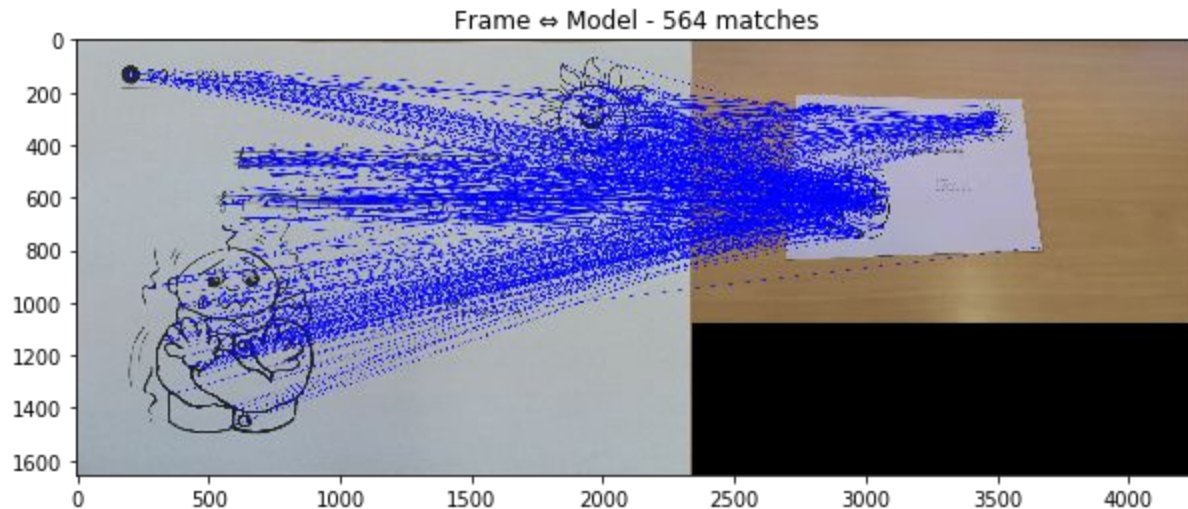
**Filters** a lot of noise.

*(Less matches, not every  $x_i$  gets a match.)*

**Costly** to compute.

# Symmetry test *aka* cross check *aka* 2-way matching

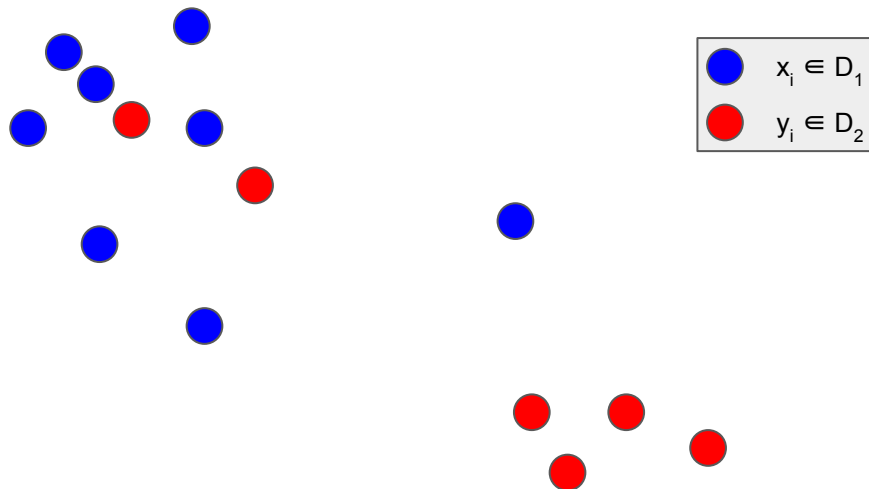
Example from next practice session



# Ratio test

For each  $x_i$  in the set of descriptors  $D_1$ , find the 2 closest elements  $y_i$  and  $y_j$  in  $D_2$ .

Keep the match  $m(x_i, y_i)$  *only if*  $\text{dist}(x_i, y_i) < \text{RATIO} * \text{dist}(x_i, y_j)$

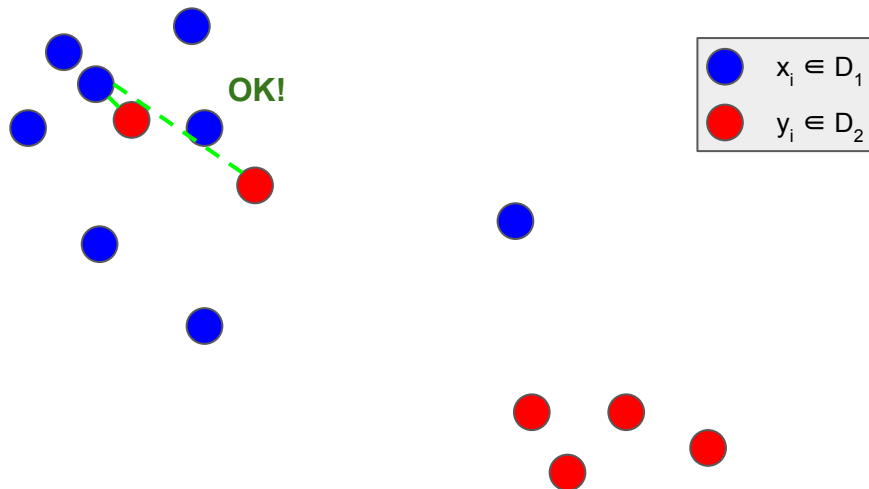


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Assume  $\text{RATIO} = \frac{2}{3}$

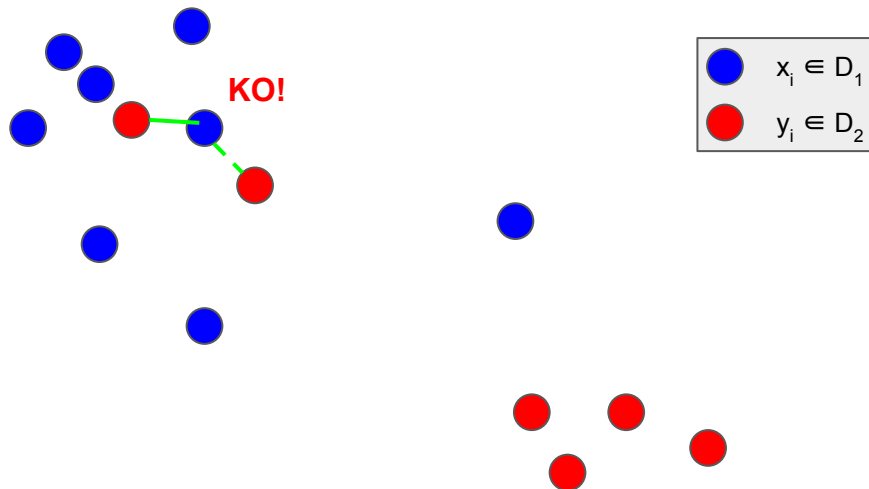


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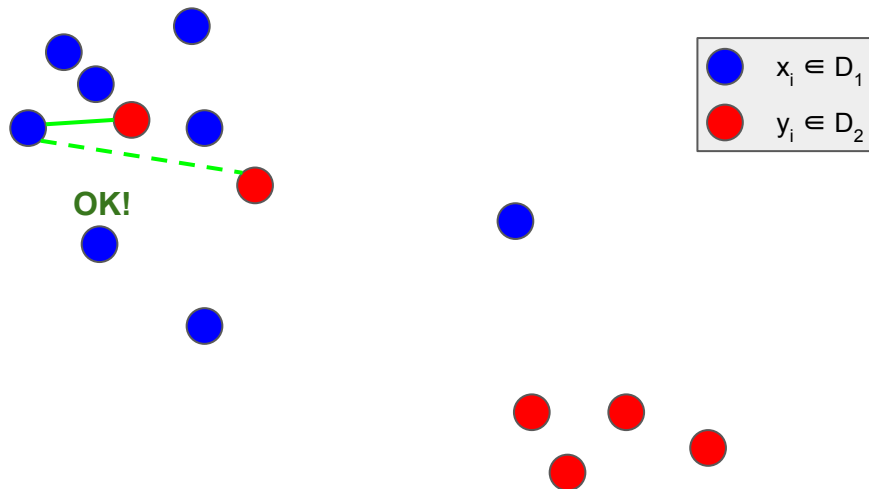


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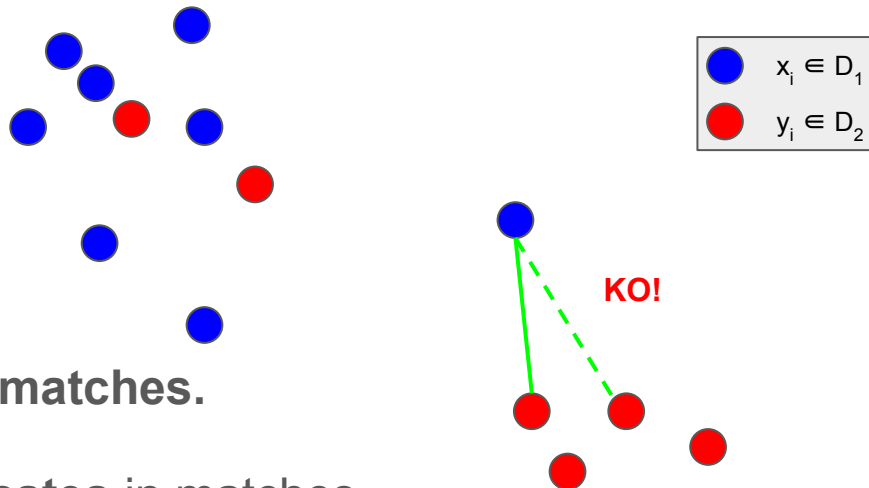


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Assume  $\text{RATIO} = \frac{2}{3}$



Good filter which **removes ambiguous matches**.

Like 1-way matching, **potential  $y_i$  duplicates** in matches.

Can be made symmetrical.



# Ratio test: calibrate the ratio

Adjust it on a training set!

For each correct/incorrect match in your annotated database, plot the *next to next closest distance* PDF.

***What is a good ratio in D. Lowe's experiment? →***

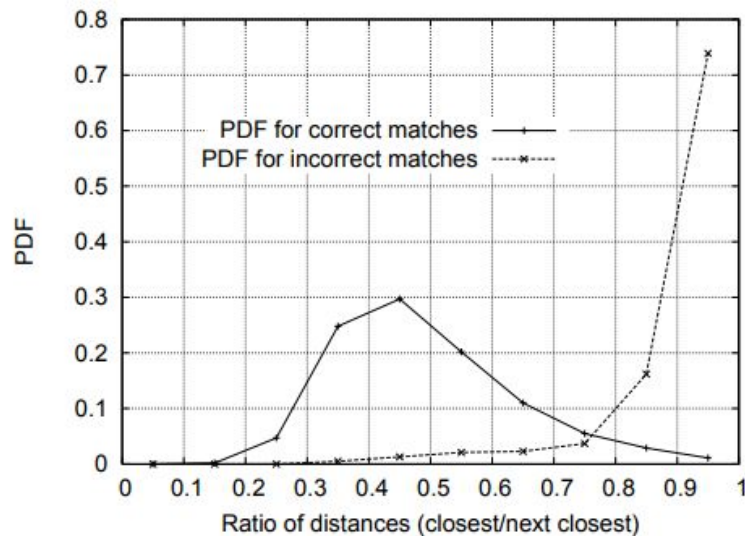
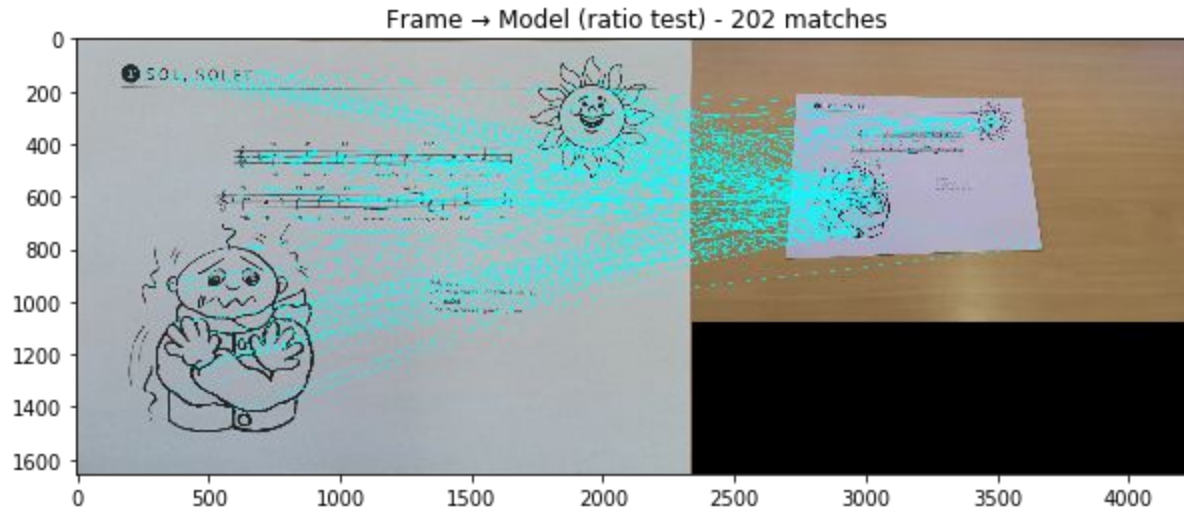


Figure 11: The probability that a match is correct can be determined by taking the ratio of distance from the closest neighbor to the distance of the second closest. Using a database of 40,000 keypoints, the solid line shows the PDF of this ratio for correct matches, while the dotted line is for matches that were incorrect.

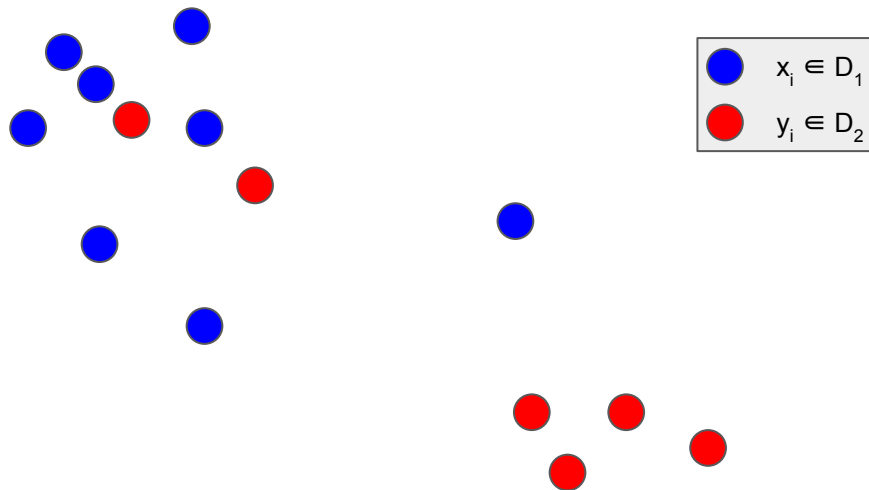
# Ratio test

Example from next practice session



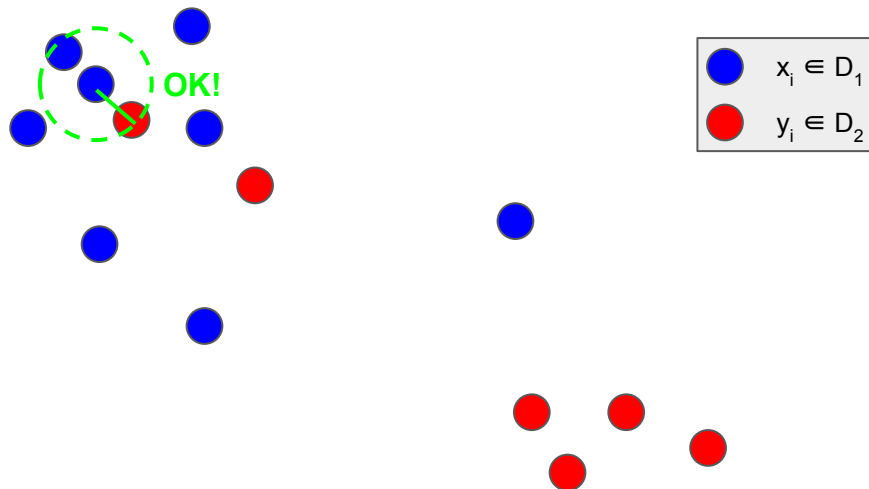
# Radius threshold

For each  $x_i$  in the set of descriptors  $D_1$ , find the closest element  $y_i$  in  $D_2$  and make sure  **$\text{dist}(x_i, y_i) < \text{RADIUS}$** .



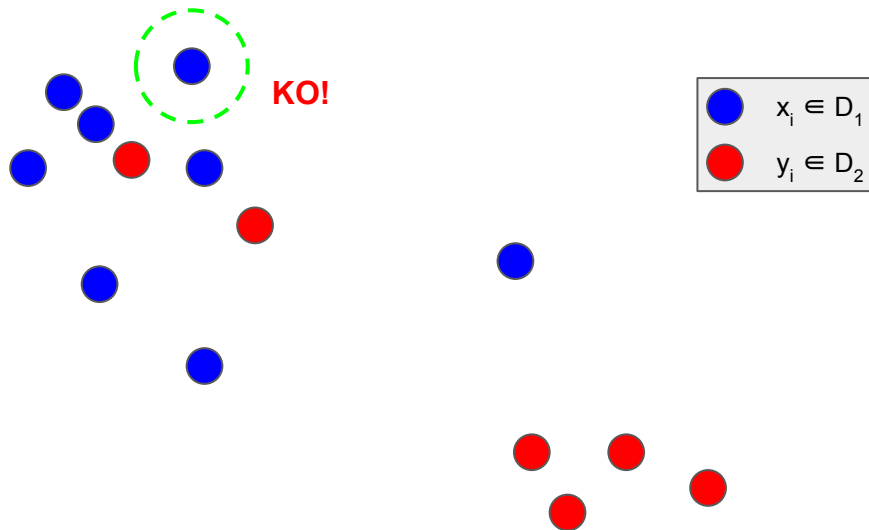
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# Radius threshold

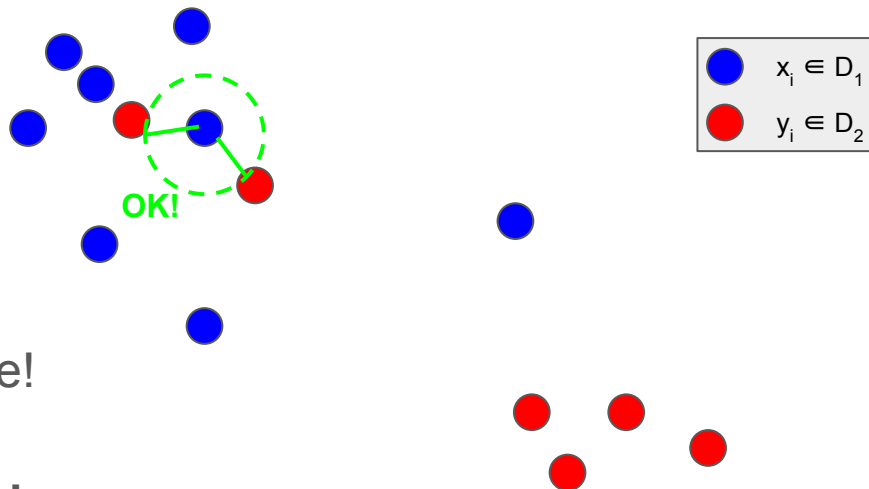
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May allow *multiple good matches*  
for some  $x_i$



## Harder to calibrate

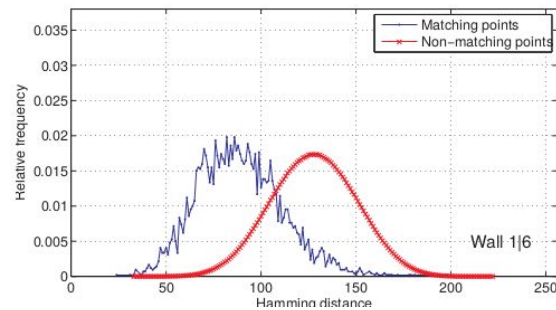
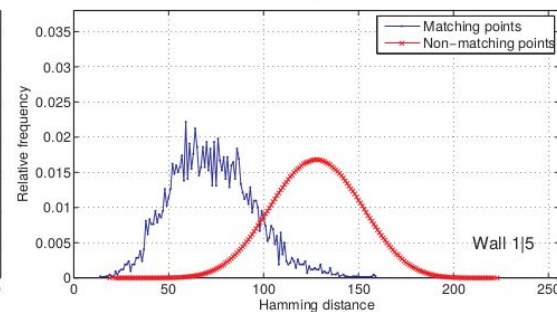
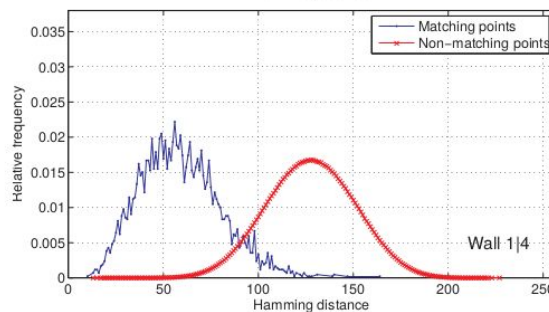
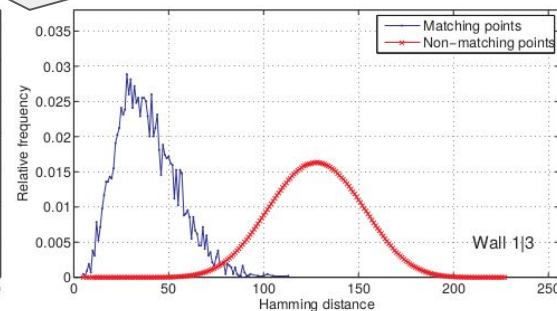
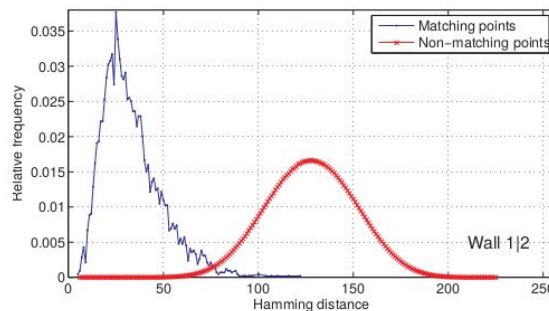
- 1 absolute value for all descriptor space!
- Usually req. a “background model”
  - = a set  $D_3$  with **only incorrect matches**

But how to query within a certain distance efficiently? **Indexing!**

# Radius threshold

*From BRIEF paper.*

If we have a background model which give us the red curve for each case (not knowing the blue one), **can we choose a good radius?**



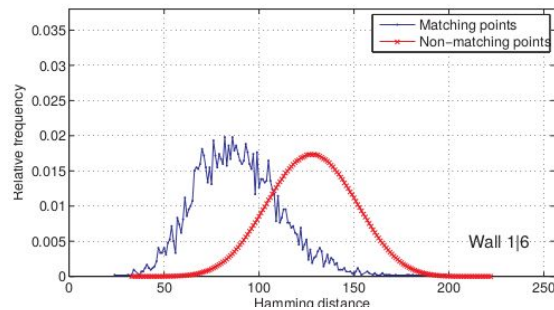
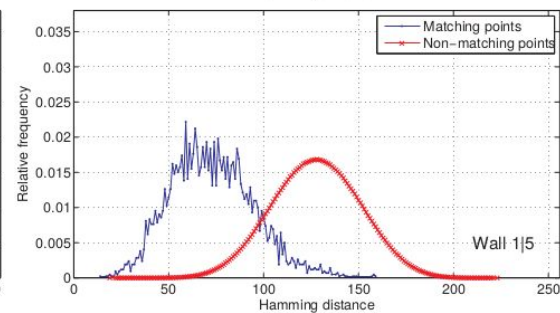
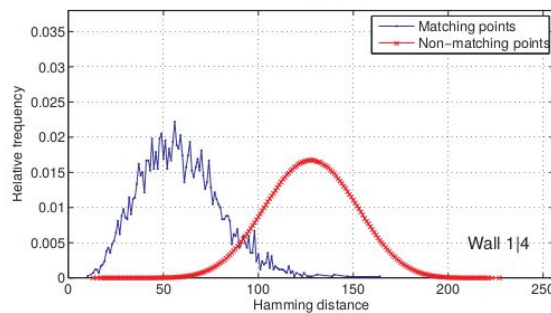
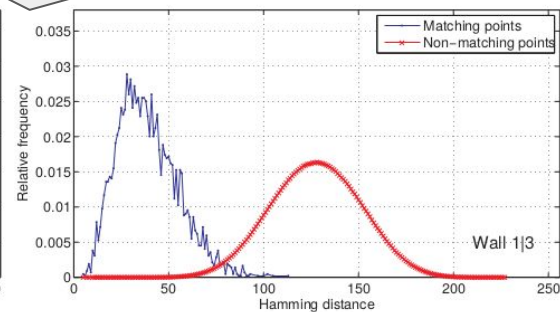
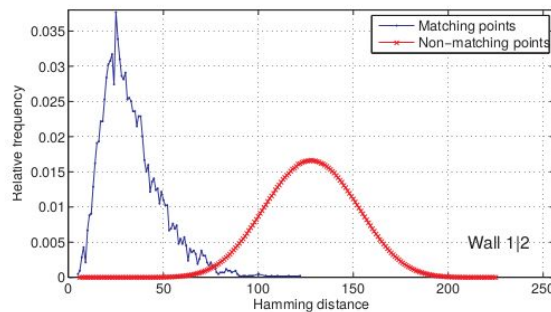
# Radius threshold

*From BRIEF paper.*

If we have a background model which give us the red curve for each case (not knowing the blue one), **can we choose a good radius?**

75-125 seems good here!

Absolute values here.





# Radius threshold

Example from next practice session

[Missing because not useful for this session]

[and tricky to handle multiple good matches]

# Geometric validation

What about the coordinates of the keypoints?

Once we have a list of matches  $\mathbf{m}(\mathbf{x}_i, \mathbf{y}_i)$ , we can check whether the coordinates of the keypoints of the matched descriptors describe a consistent mapping from one position to another.

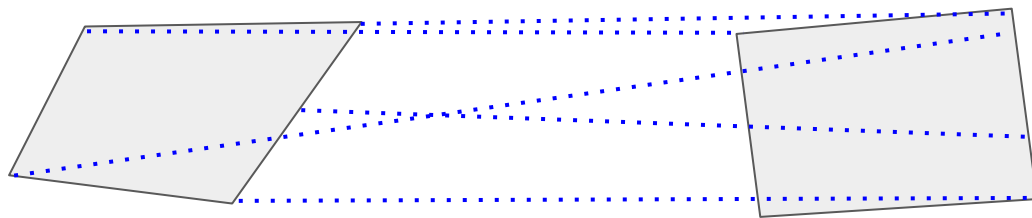
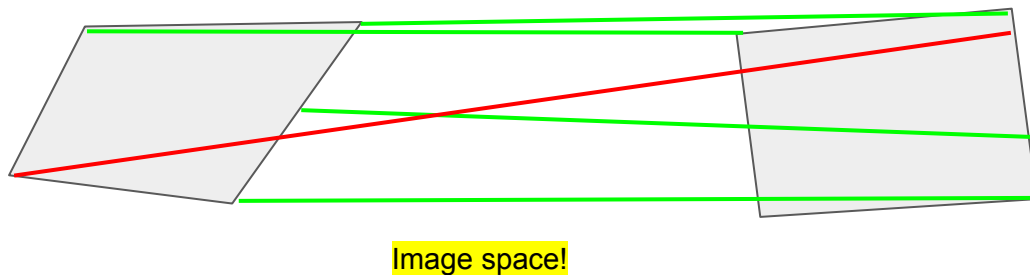


Image space!

# Geometric validation

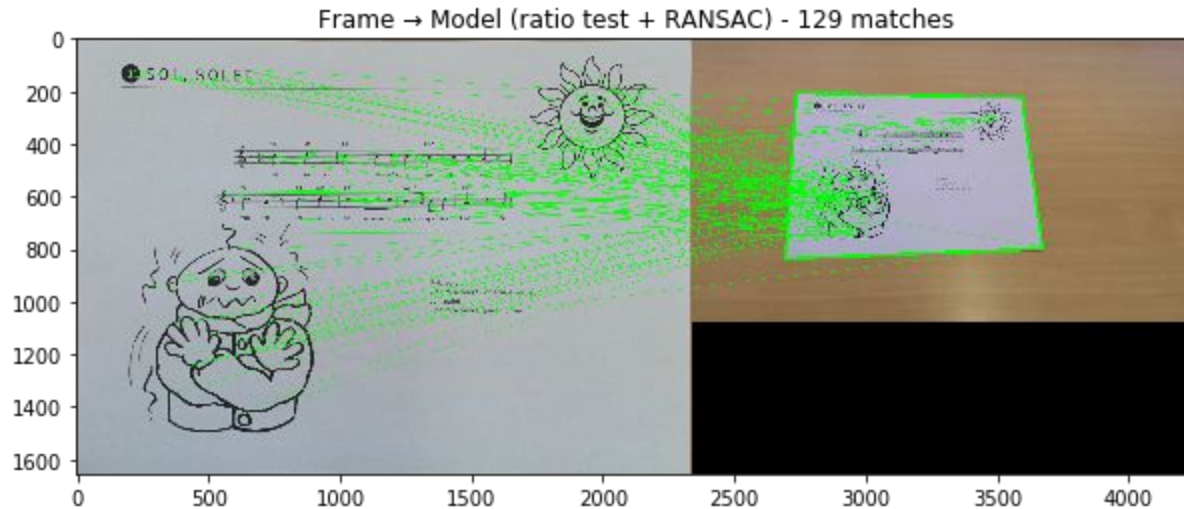
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# Geometric validation

Example from next practice session



# Geometric validation

## How to check the consistency of the transformation?

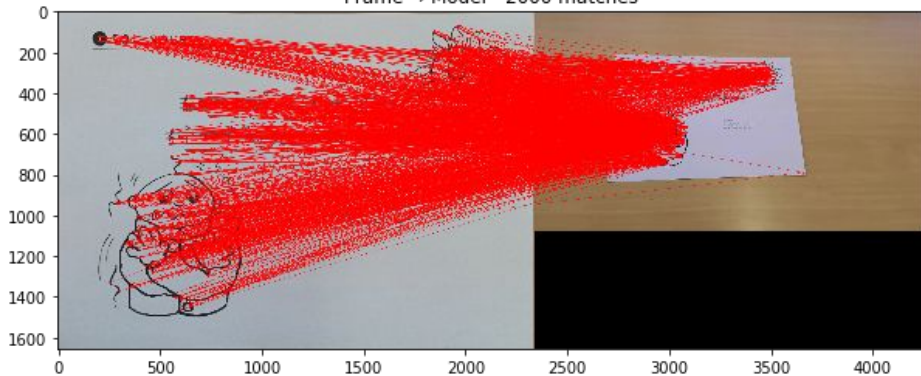
Difference classes for transformations.

Different methods to estimate them and check which matches agree and disagree.

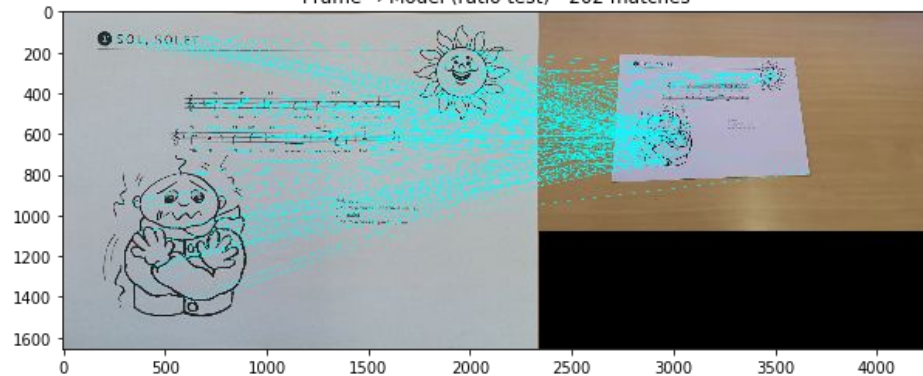
⇒ Next lecture parts.

# Summary of matching techniques (for practice session)

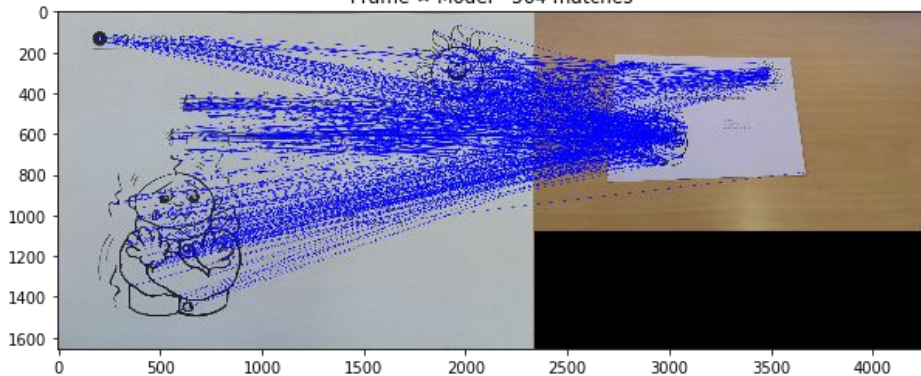
Frame → Model - 2000 matches



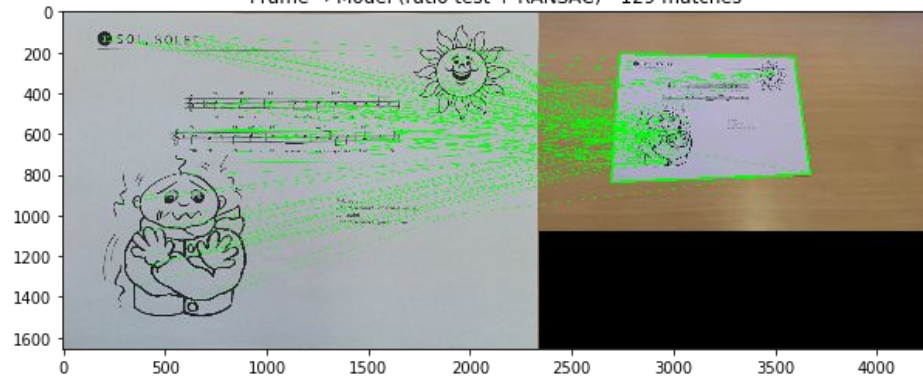
Frame → Model (ratio test) - 202 matches



Frame ⇌ Model - 564 matches



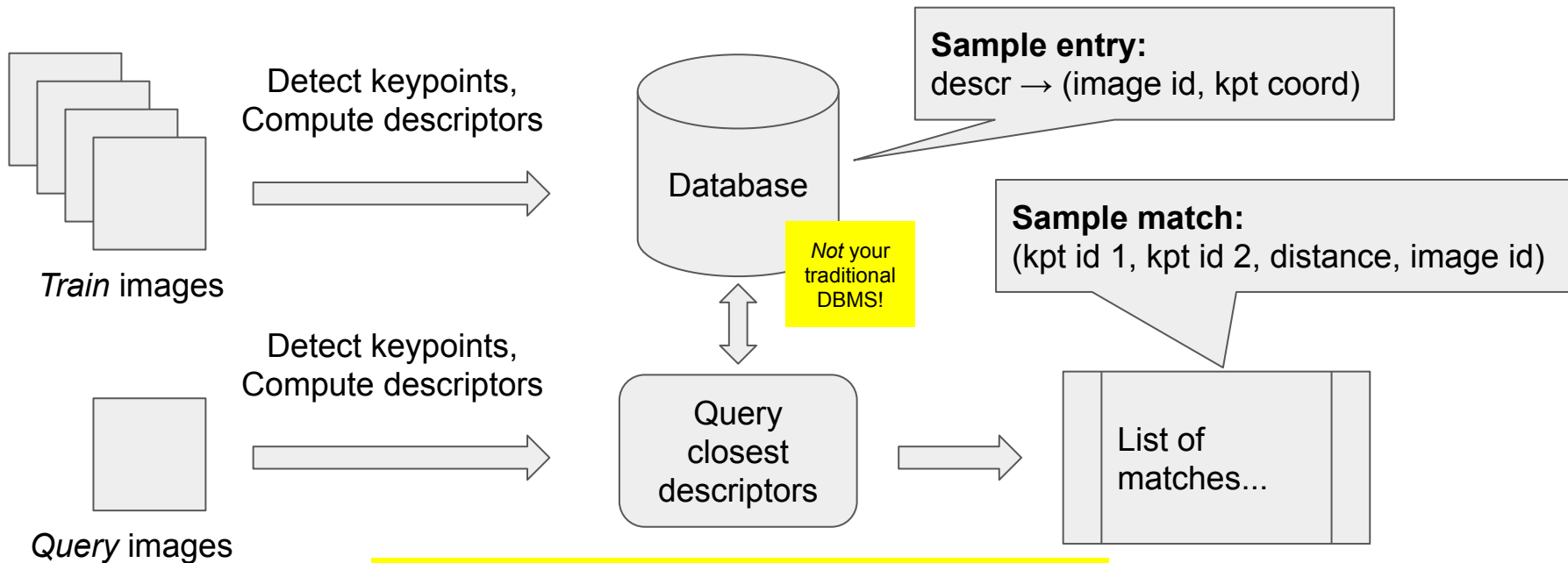
Frame → Model (ratio test + RANSAC) - 129 matches



# Indexing

# Indexing pipeline

Use case: We have a database of images and we want to find an object from it.



How can we get the **closest** descriptors?



# Bruteforce matching *aka* linear matching

*Simply scan all data and keep the closest elements.*

Does not scale to large databases, but can be faster on small ones!

*Especially with fast distance measures, like Hamming.*

Exact matching. Global optimum guarantee.

Supports cross check (double scan).

# Indexing

Build one+ indexes of descriptors → descriptor data

Indexing is often approximate (especially if asking for more than 1 neighbor), because :

1. Databases can grow very large
2. Descriptor spaces have many dimensions

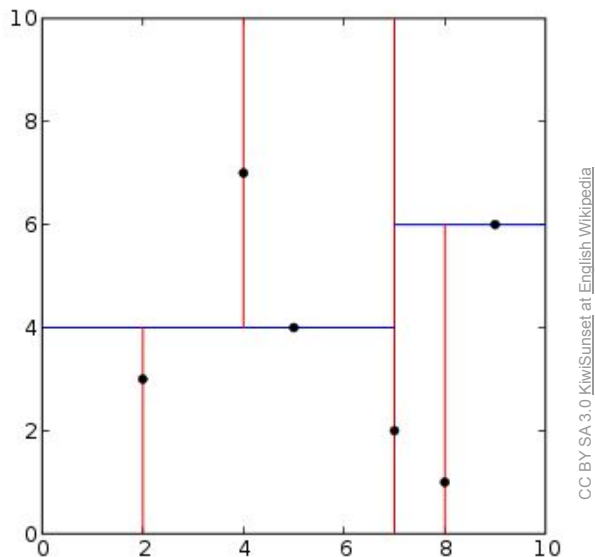
Exact matching and global optimum are **not always guaranteed**.

Also, cross check usually does not make sense and is therefore not implemented.

Usually, we start by **reducing the dimension / encoding our features** (*next lecture*)

# kD-Trees

*The  $k$ -d tree is a binary tree in which every leaf node is a  $k$ -dimensional point.*



# kD-Trees

*The k-d tree is a binary tree in which every leaf node is a k-dimensional point.*

**Construction:** for each dimension, recursively split the space to maximize data separation until a maximum size is reached

**Retrieval:** compute the leaf node of each query, then explore points in the leaf and in siblings / parents if not satisfying (boundaries not within radius of the query ball)

**Complexity:** asymptotic  $O(\log N)$  when  $N \gg 2^k$

In practice, kD-trees do not work for searching in high dimensions.

# FLANN – Efficient indexing

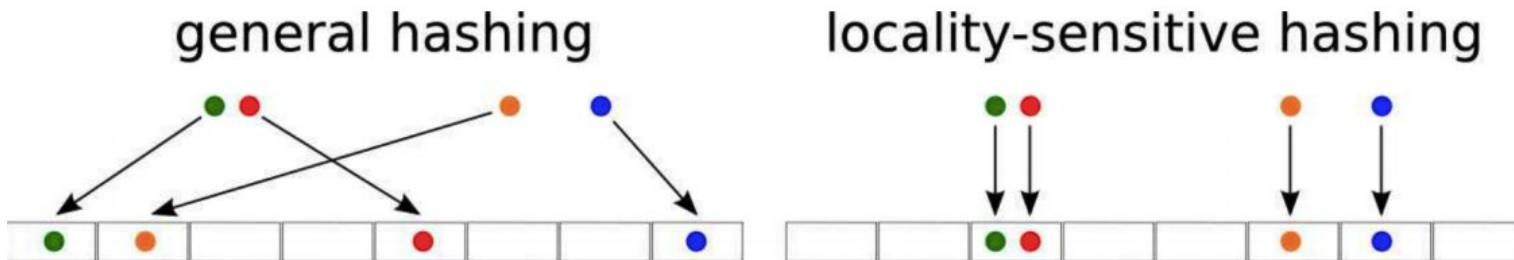
Original version: hierarchical k-Means.

Construction: repetitive k-Means on data (then inside clusters) until minimum cluster size is reached.

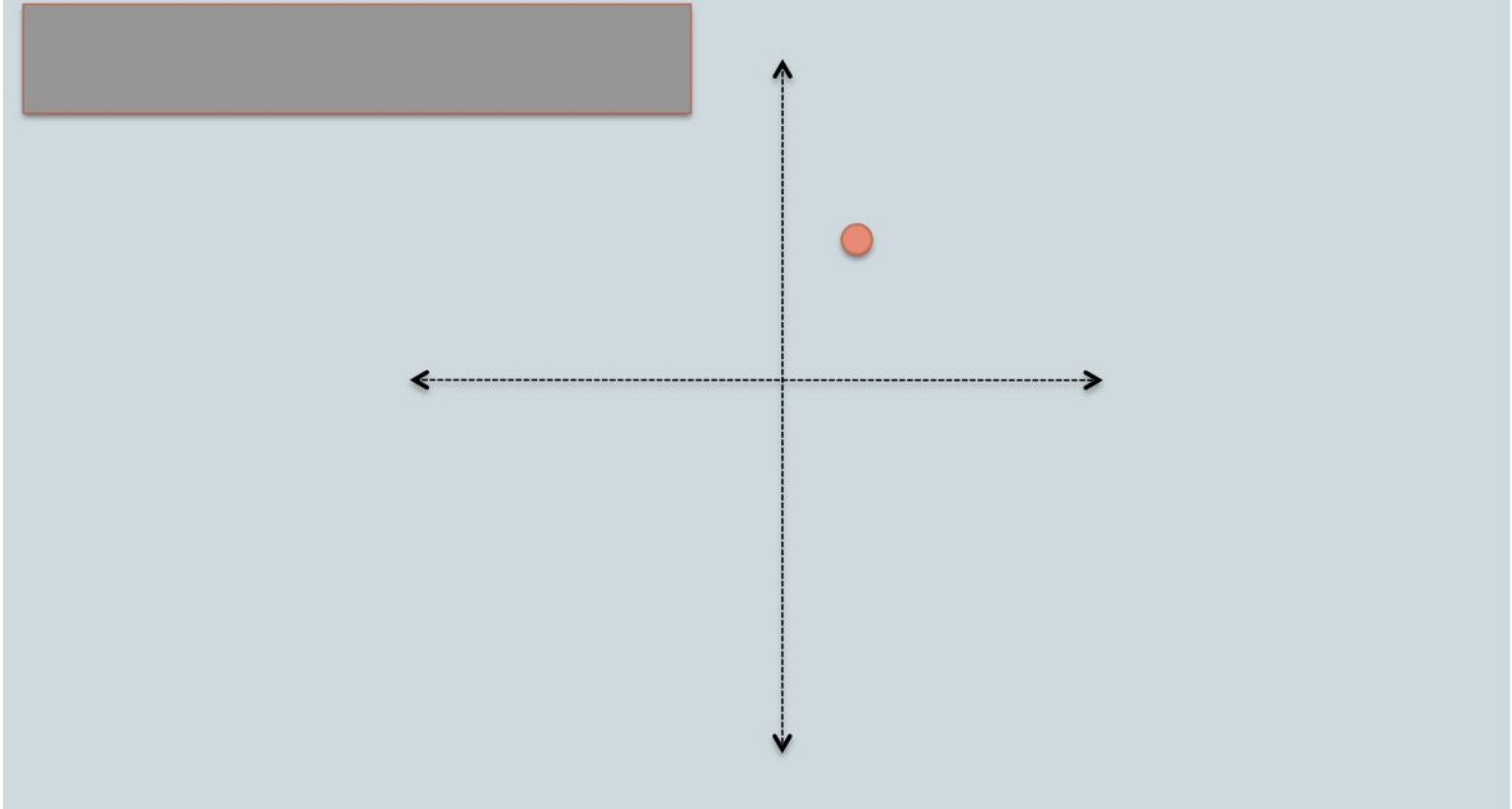
Lookup: traverse the tree in a best-bin-first manner with backtrack queue, backtrack until enough points are returned

# Locality Sensitive Hashing (LSH)

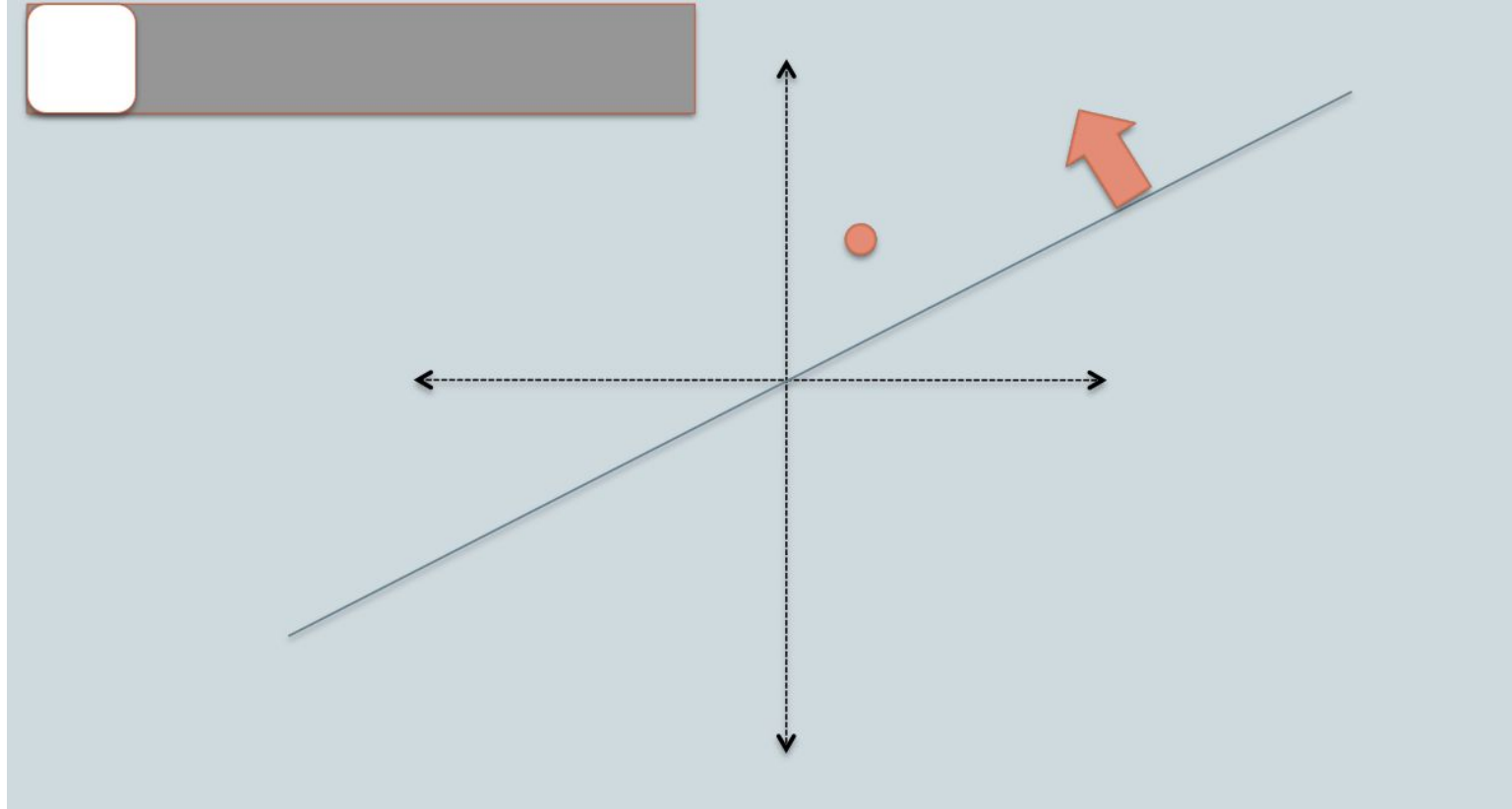
Hash items using a family of hash function which project similar items in the same bucket with high probability. **NOT cryptographic hashing!**



# Locality Sensitive Hashing (LSH)

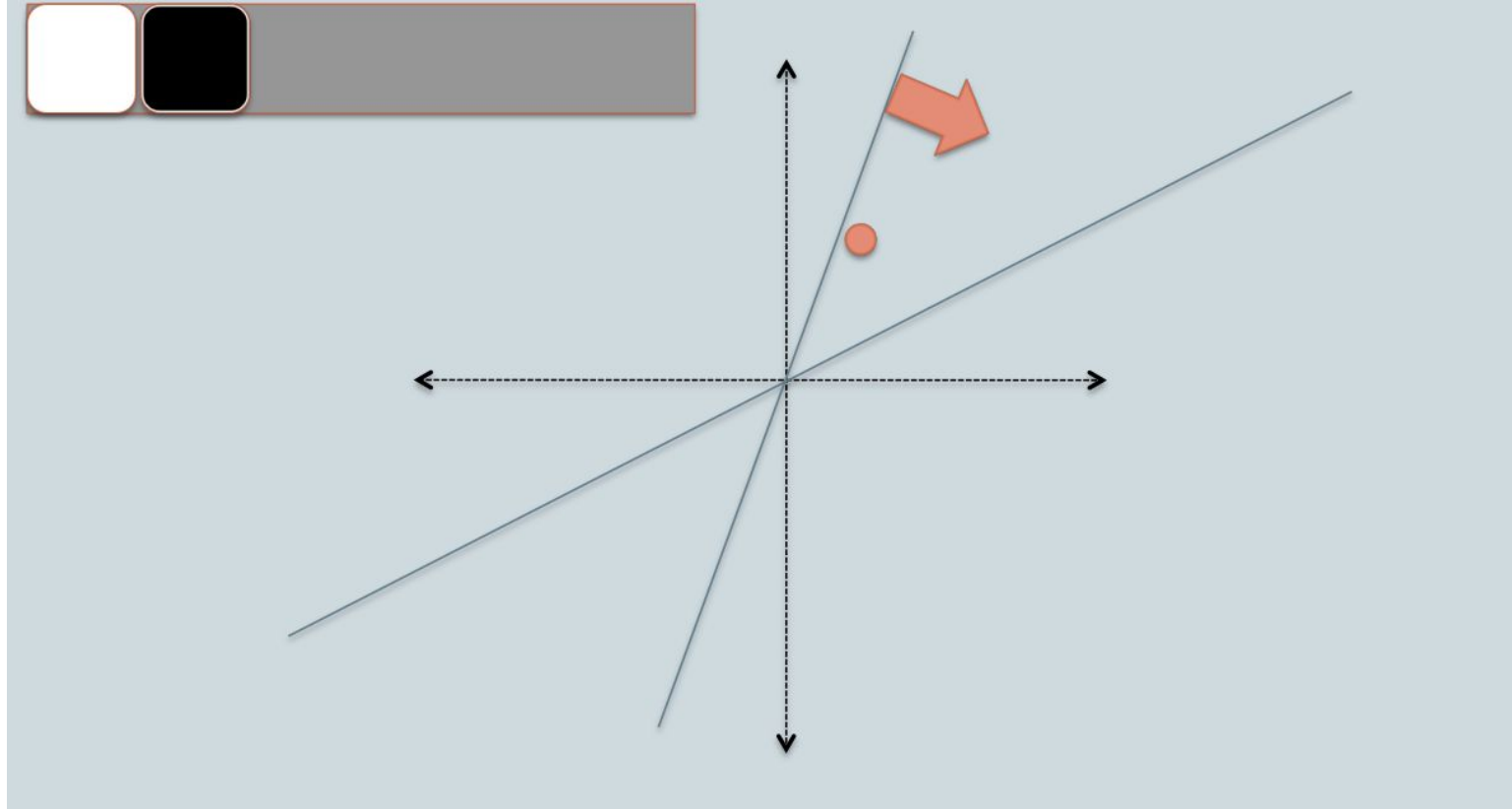


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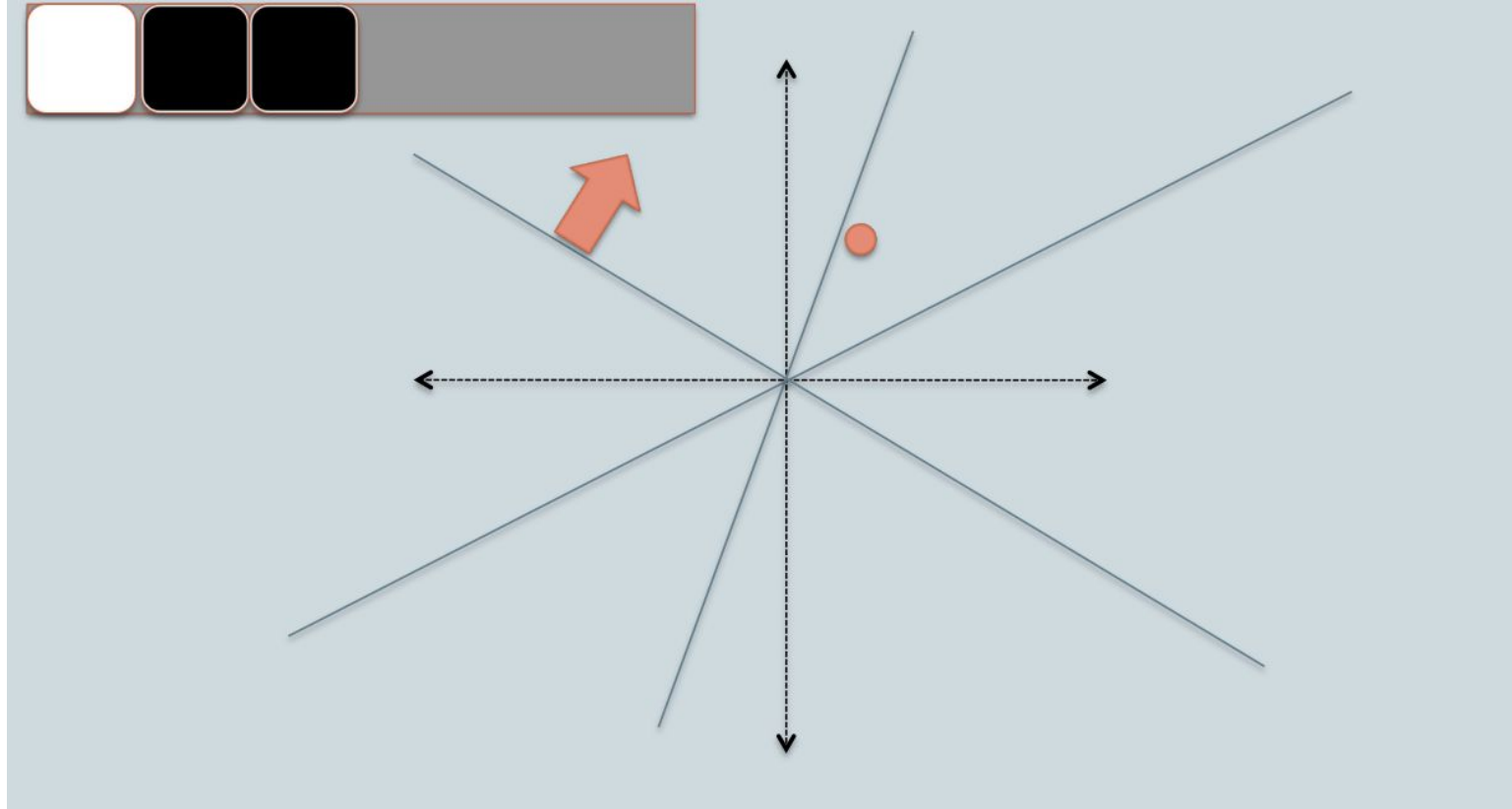




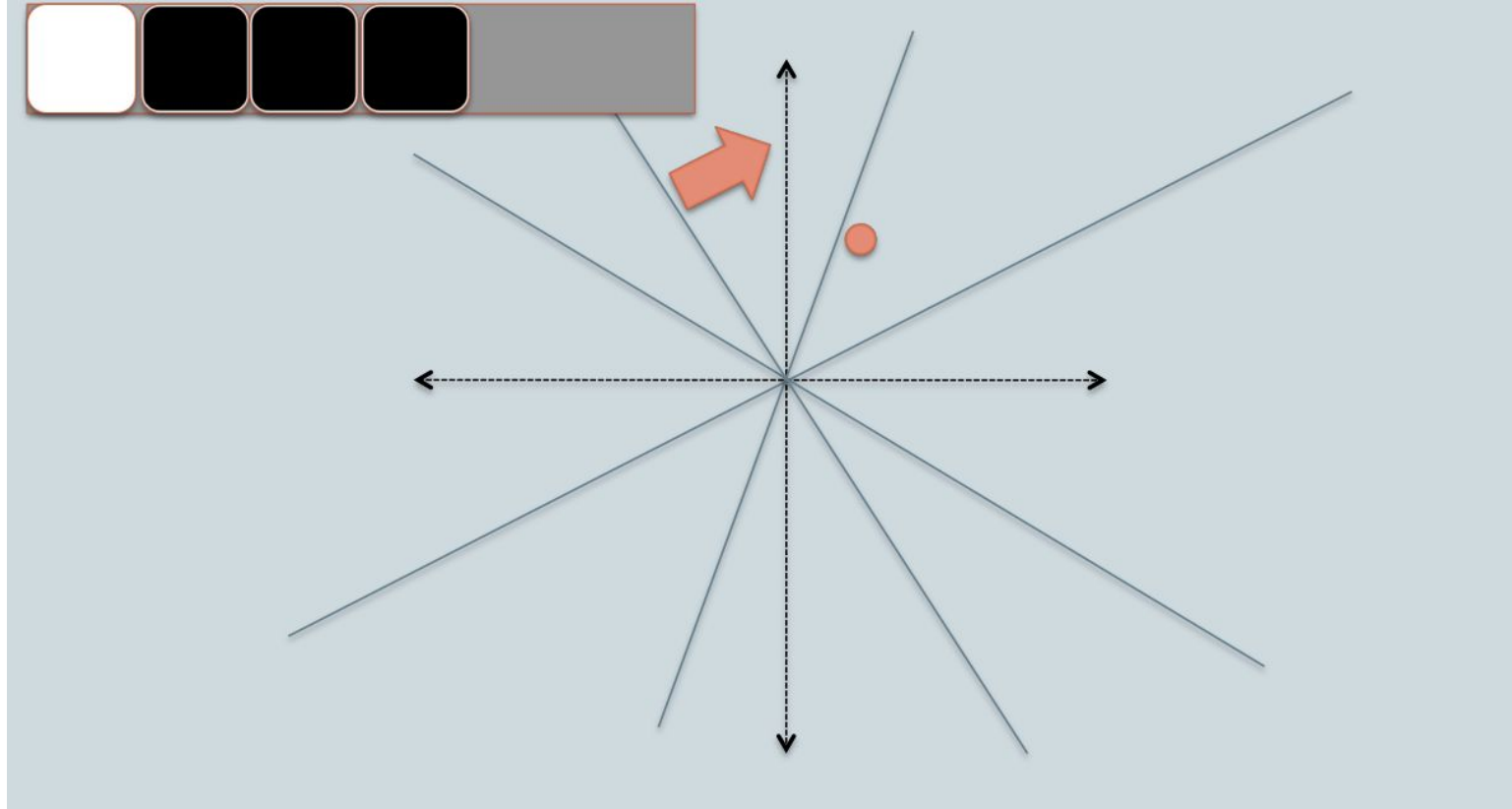
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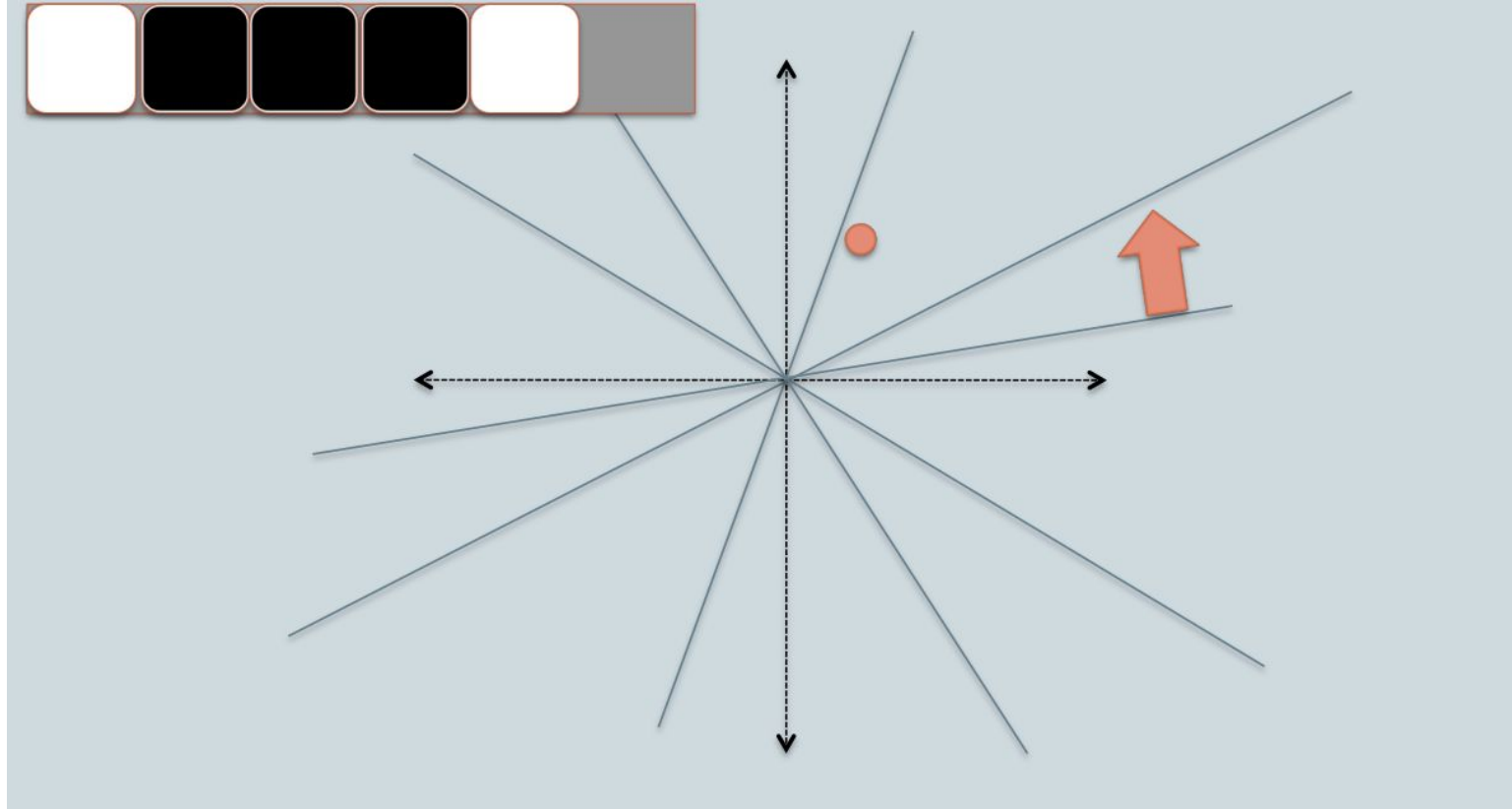
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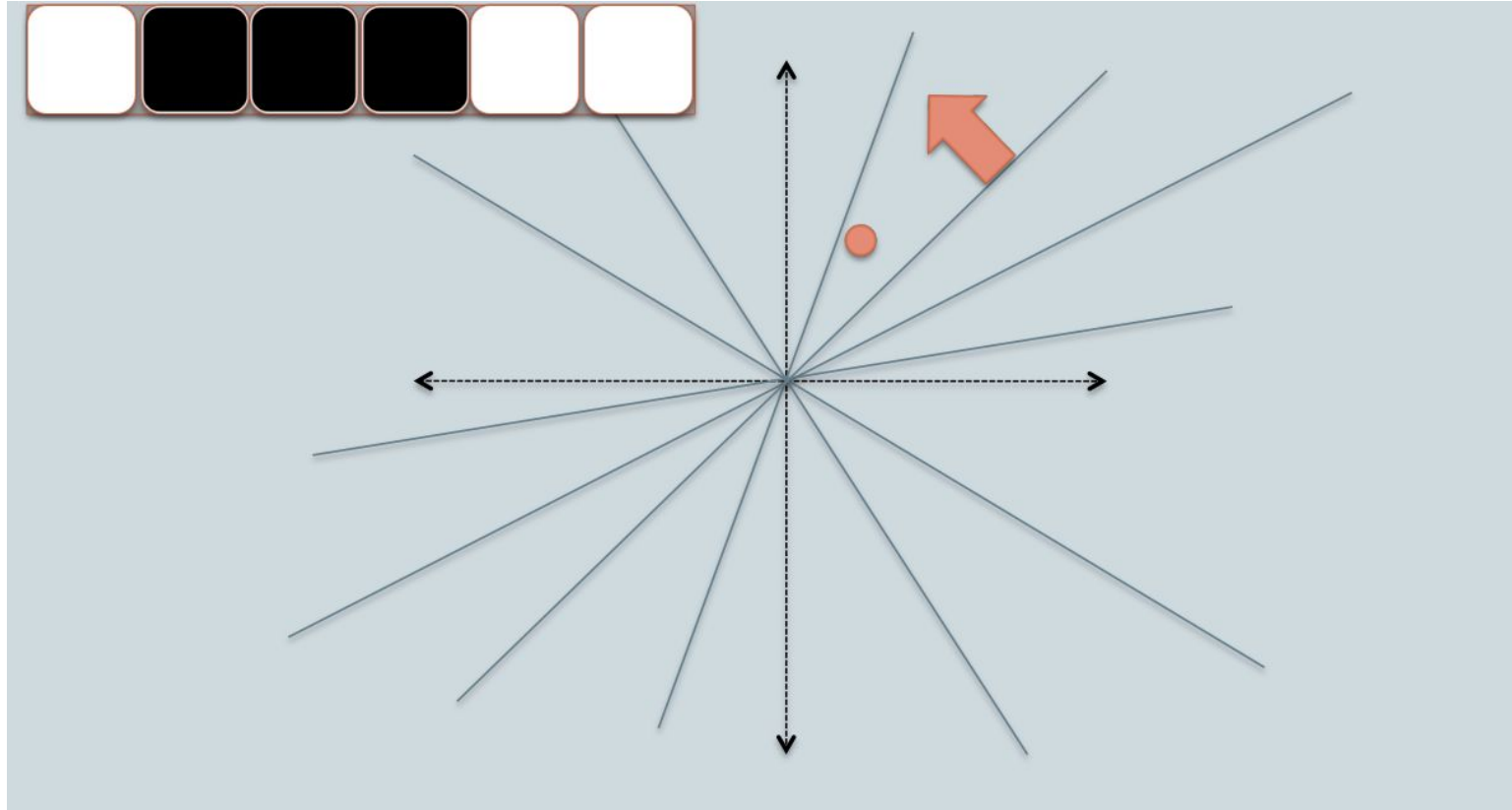
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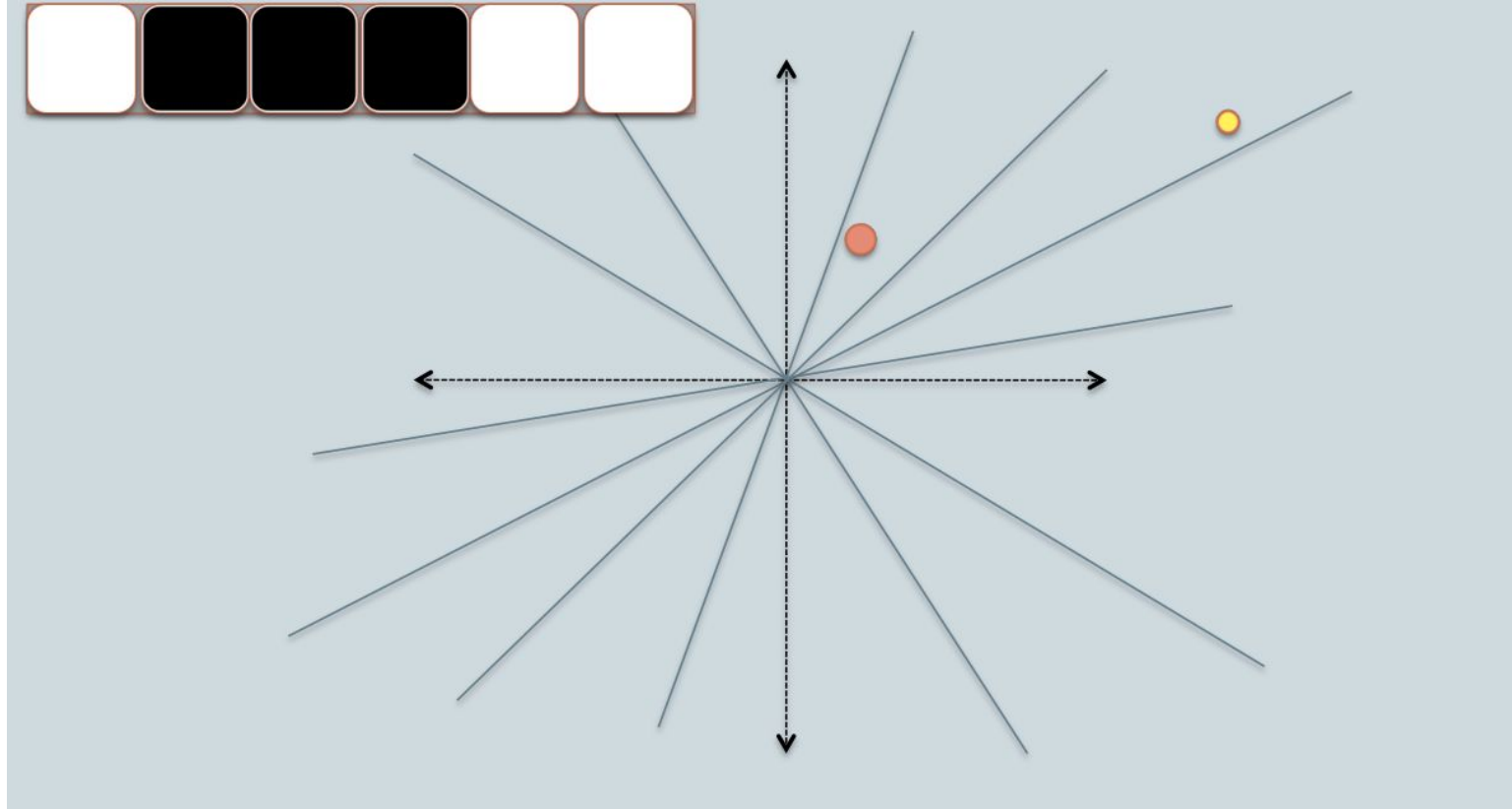
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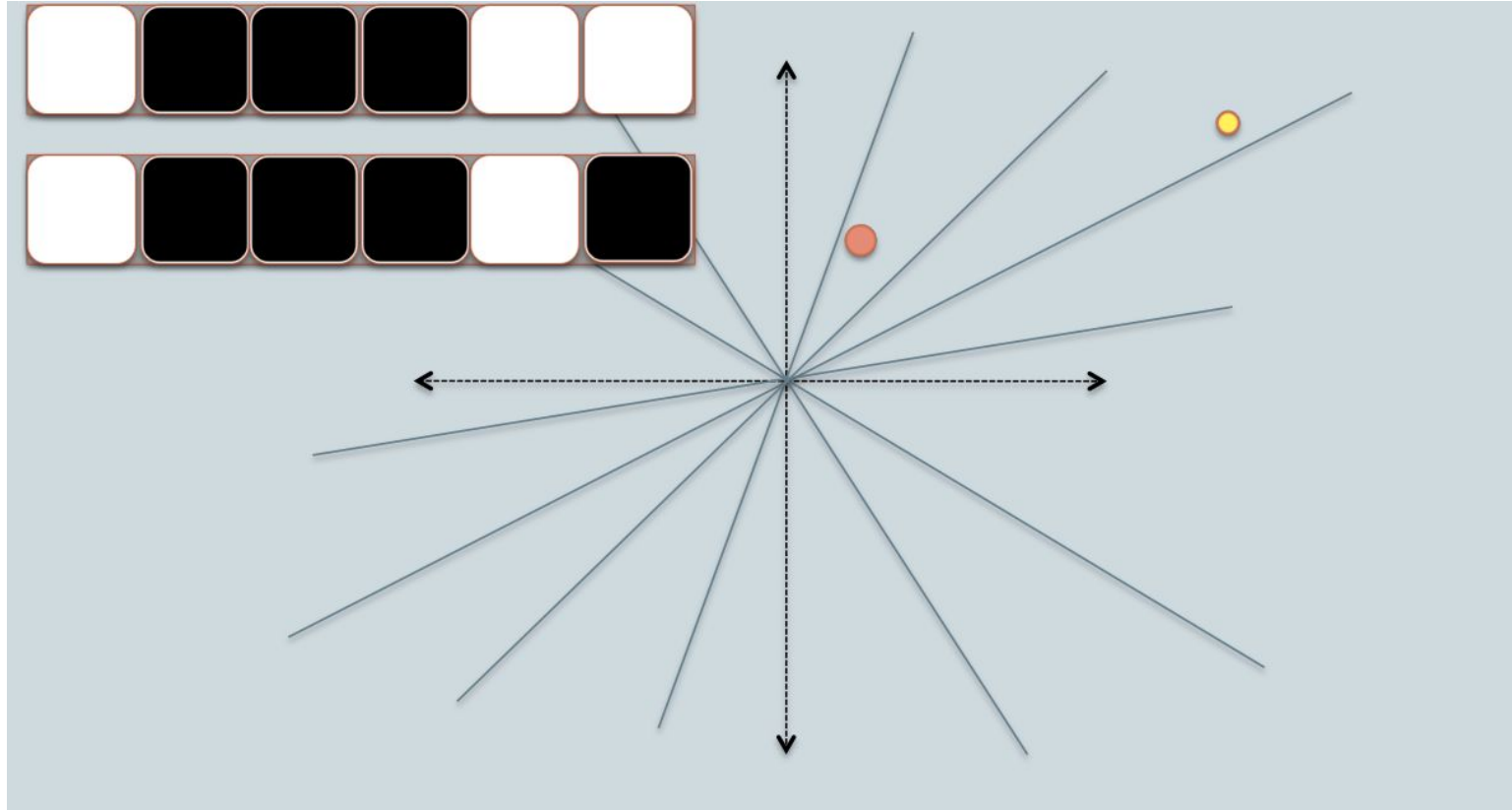
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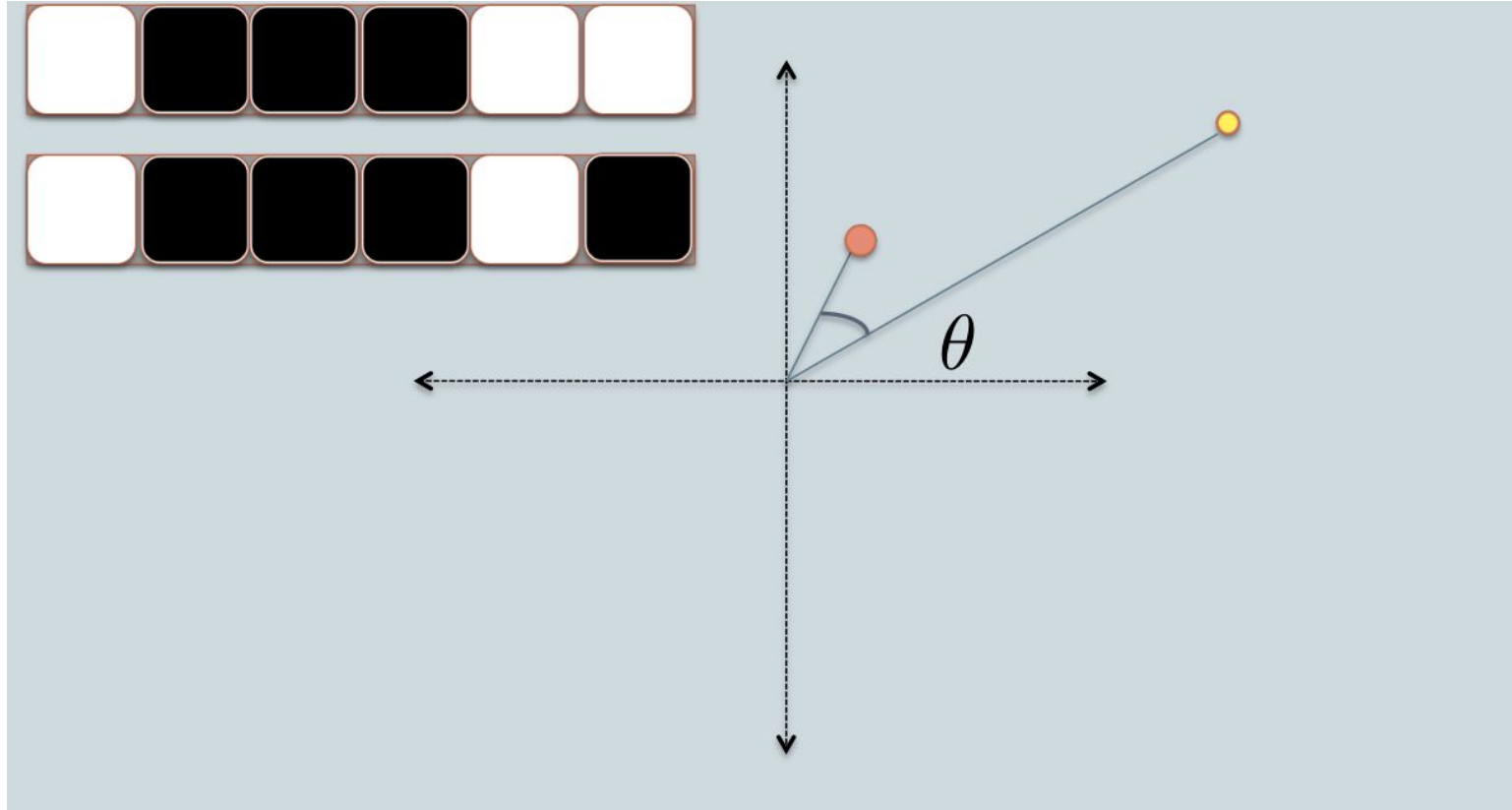
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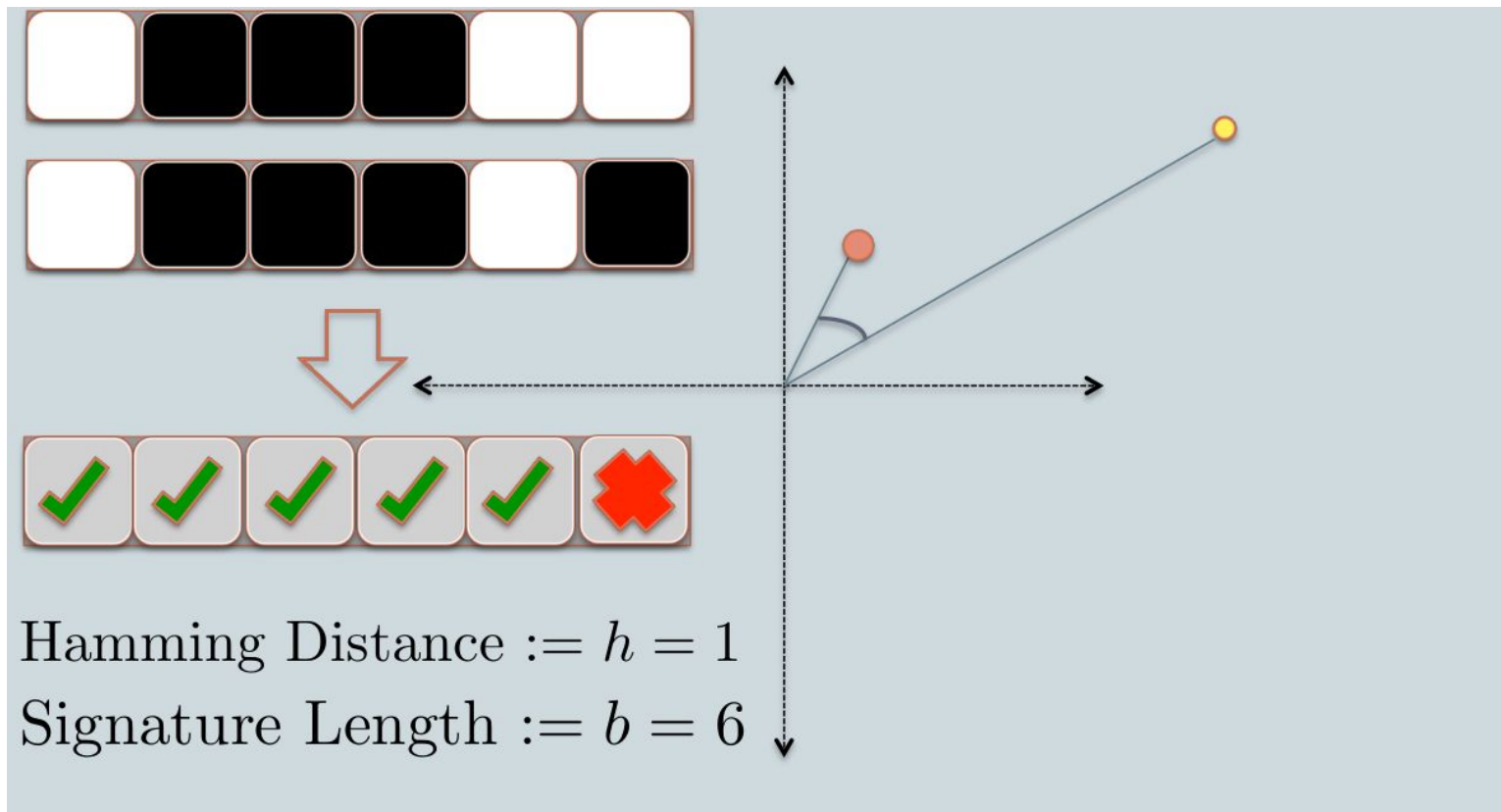


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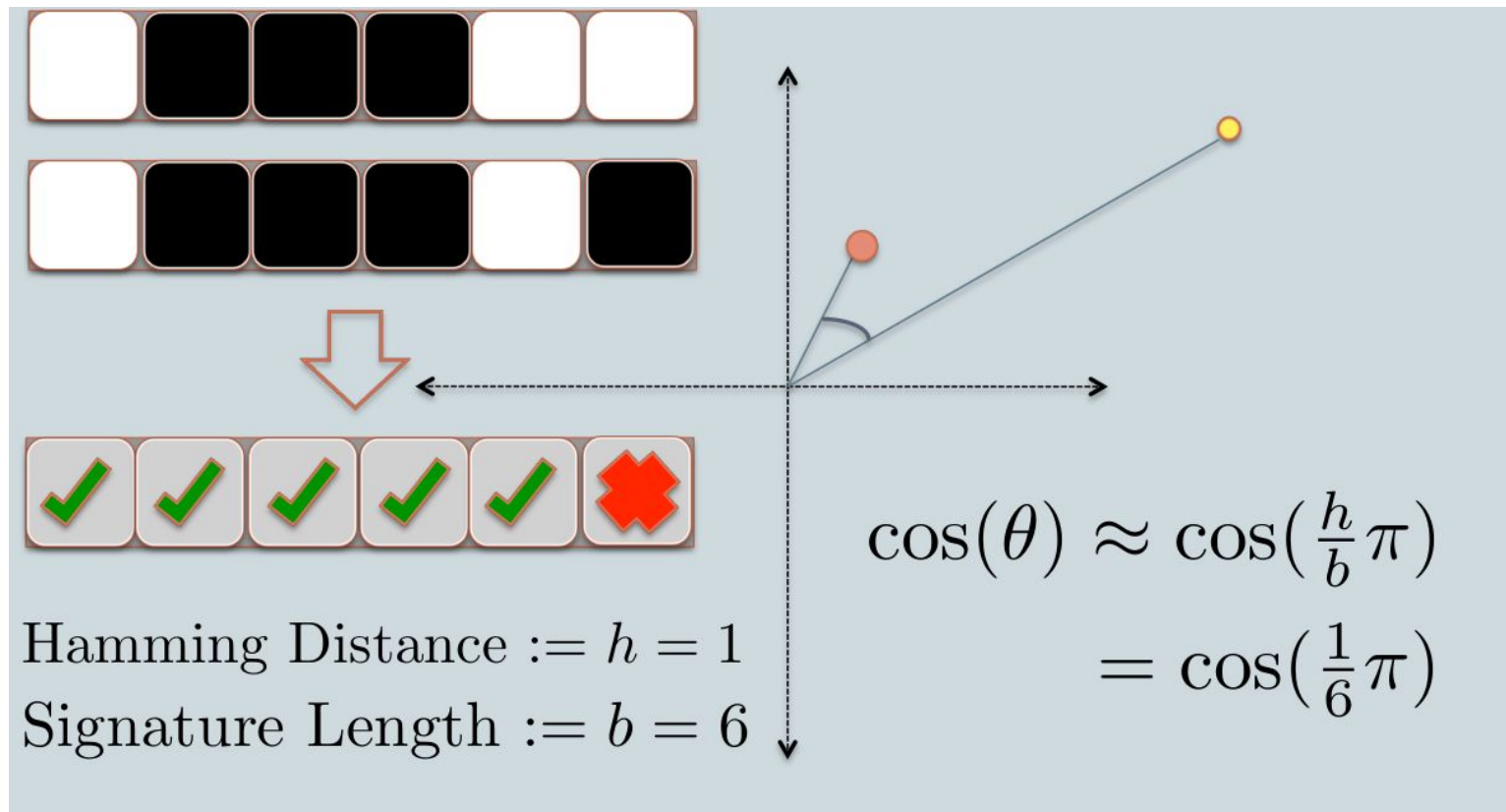




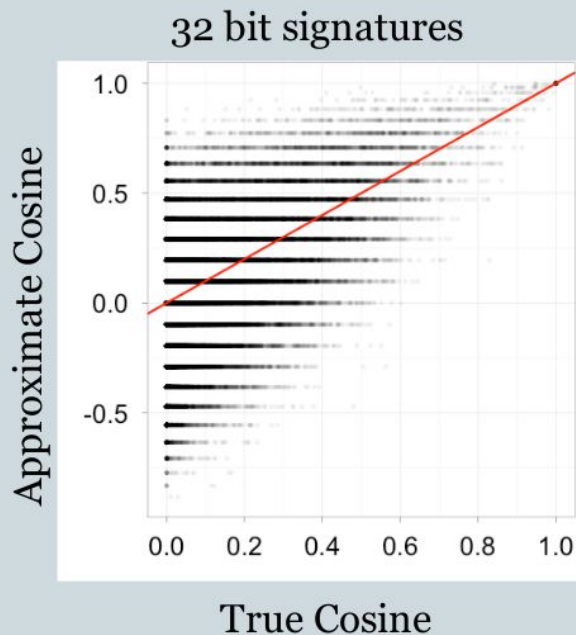
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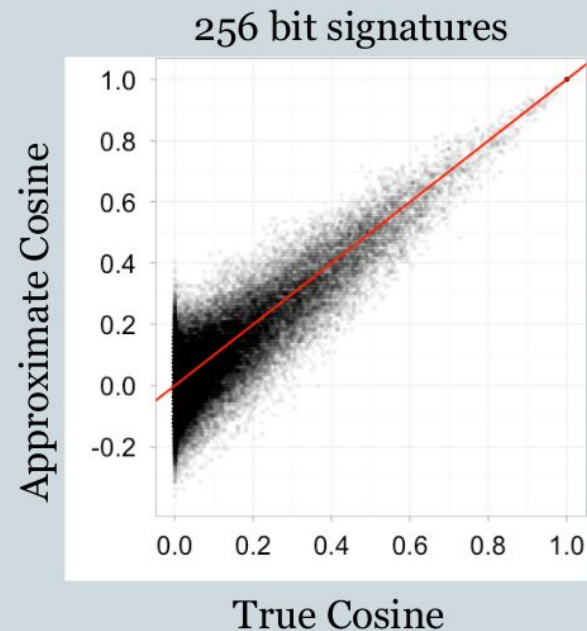
# Locality Sensitive Hashing (LSH)



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**Cheap**



**Accurate**

# Locality Sensitive Hashing (LSH)

Fast and efficient with large spaces, lot of data.

Return a “good match”, maybe not the best one.

kNN can be costly (scan other bins).

Indexes binary descriptors very straightforwardly using bit sampling (sample bits from the coordinates).

Random projections for other cases, or other techniques...

# Which indexing?

Experiment.

Advices for practice session:

- Use **bruteforce/linear** for first experiments / best (but slow) results
- Use **LSH** for **binary descriptors** like ORB
- Use **randomized kD-Trees** with SIFT (**integer descr.** with similar dimension) for **moderate** dataset size,  
**k-Mean tree** otherwise

