# MLRF Lecture 04 J. Chazalon, LRDE/EPITA, 2021

# **IR** evaluation

Lecture 04 part 03

#### How to evaluate a retrieval system?

We need a set of queries for which we know the expected results "Ground truth", aka "targets", "gold standard"...

To compare 2 methods, we need to use the same database and the same queries.

Many measures / indicators.

Core criterion: is a result relevant (binary classification)?

#### **Precision and Recall**

Used to measure the balance between

- Returning many results, hence a lot of the relevant results present in the database, but also a lot of noise
- Returning very few results, leading to less noise, but also less relevant results

#### **Precision and Recall**

Precision (P) is the fraction of retrieved documents that are relevant

 $Precision = \frac{\#(relevant items retrieved)}{\#(retrieved items)} = P(relevant|retrieved)$ 

Recall (R) is the fraction of relevant documents that are retrieved

 $Recall = \frac{\#(relevant items retrieved)}{\#(relevant items)} = P(retrieved|relevant)$ 

	Relevant	Nonrelevant
Retrieved	true positives (tp)	false positives (fp)
Not retrieved	false negatives (fn)	true negatives (tn)

$$P = tp/(tp+fp)$$
  

$$R = tp/(tp+fn)$$

#### F-measure

F measure is the weighted harmonic mean of precision and recall

$$F = \frac{1}{\alpha \frac{1}{P} + (1 - \alpha) \frac{1}{R}} = \frac{(\beta^2 + 1)PR}{\beta^2 P + R} \quad \text{where} \quad \beta^2 = \frac{1 - \alpha}{\alpha}$$

where  $\alpha \in$  [ 0, 1 ] and thus  $\beta^{_2} \in$  [ 0,  $\infty$  ]

The default value is  $\beta = 1$ , leading to:

$$F_{\beta=1} = \frac{2PR}{P+R}$$

#### How to evaluate a <u>ranked</u> retrieval system?

When results are ordered, more measures are available.

Common useful measures are:

- The precision-recall graph and the mean average precision
- The ROC graph and the area under it (AUC)

#### Precision-recall graph

**Plotting the points** 

For a given query For each result

if the result is relevant
set x = #tp / #expected
set y = #tp / #returned

1.0 0.8 Precision 0.6 0.4 0.2 0.0 0.2 0.8 0.0 0.4 0.6 1.0 Recall

The recall always increases while we scan the result list.

#### Equal Error Rate and Average Precision

Note: the PR graph does not provide a total order ⇒ need more indicators





#### Mean average precision at k — mAP (@k)

Mean of the average precision of several queries, when considering **k results for each query** 

 $\Rightarrow$  makes evaluation tractable with very large databases

Computed for each query using the <u>trapezoid technique</u>  $\rightarrow$ 

#### General algorithm:

For each query q<sub>i</sub> in the test set with expected results e<sub>i</sub>: Retrieve the list ret<sub>i</sub> of k best results Compute the AP ap<sub>i</sub> given e<sub>i</sub> and ret<sub>i</sub>
Compute the mean AP over all ap<sub>i</sub>



#### Example: Compute the AP for a given query

For this query and the following results, plot the precision/recall graph and compute the average precision.















Check the first result: It it relevant?



R





Check the **first** result: It it relevant? YES 6 ⇒ Compute current precision: 1 relevant / 1 retrieved = 1  $\Rightarrow$  Recall = 1 relev. /3 expected =  $\frac{1}{3}$ 0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2 0.1 0  $\frac{1}{3}$  $\frac{2}{3}$ N



R

Check the **next** result: It it **relevant**?





Check the **next** result: It it **relevant**? **NO** ⇒ P@2 = 1 relevant / 2 retrieved = ½ ⇒ R@2 is unchanged





Check the **next** result: It it **relevant**?





Check the next result: It it relevant? YES  $\Rightarrow$  P@3 = 2 relevant / 3 retrieved =  $\frac{2}{3}$  $\Rightarrow$  Add a point at next recall value ( $\frac{2}{3}$ )





And we keep going... P@4 = 2/4 = 1/2R@4 = unchanged





And we keep going... P@5 = 2/5 = 0.4R@5 = unchanged





Ρ

0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2 0.1 0

And we keep going... P@6 = 2/6 = 1/3R@6 = unchanged



Ρ

0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2 0.1 0

And we keep going... P@7 = 2/7 = 0.285...R@7 = unchanged



Ρ

0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2 0.1 0

And we keep going... P@8 = 2/8 = 1/4R@8 = unchanged



Ρ

0.9 0.8 0.7 0.6 0.5 0.4 0.3 0.2 0.1 0

And we keep going... P@9 = 3/9 = 1/3 R@9 = 3/3 = 1



It does not change the AP here... P@10 = 3/10 R@10 = 3/3 = 1





# Case 1: assume $|e_i| = 3$

And we are done!

A common approximation is to take only the upper envelope of the curve...



2

3

8

5

10

# Case 2: what if $|\mathbf{e}_i| = 4$ ?

1. Adjust R values.



# Case 2: what if **|e<sub>i</sub>| = 4?**

- 1. Adjust R values.
- 2. P values do not change if **k** does not change.



# Case 2: what if **|e<sub>i</sub>| = 4?**

- 1. Adjust R values.
- 2. P values do not change if k does not change.
- 3. Here, it would imply that we did not get all relevant results (very common in practice) ⇒ we stop the curve before the 1



#### ROC & others

[next lecture, more useful for classification]

#### Ground truthing issues

Do we have to annotate all images within a dataset for all our test queries?

No! Use "distractors": samples that you know, for sure, not to be relevant to any query.